

# Global Illumination I

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What is Global Illumination?







Photo by Abigail Keenan





*Photo by Kaushik Panchal*

Ray tracing is everywhere in VFX & animation industry!

# The State of Rendering







*Manuka Renderer*



Disney · PIXAR  
RenderMan





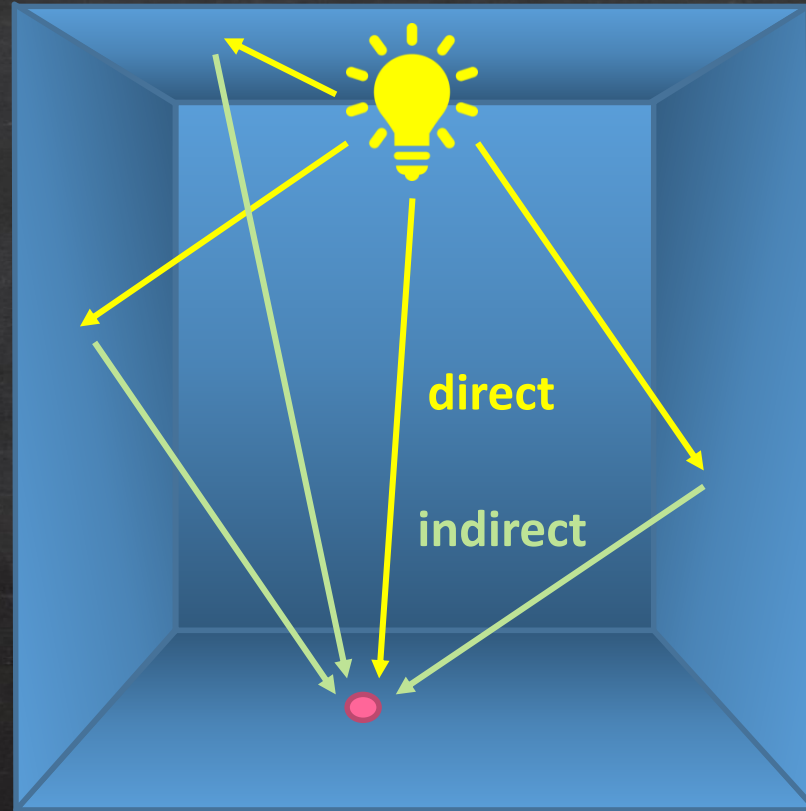
SOLIDANGLE

[arnold renderer](#)



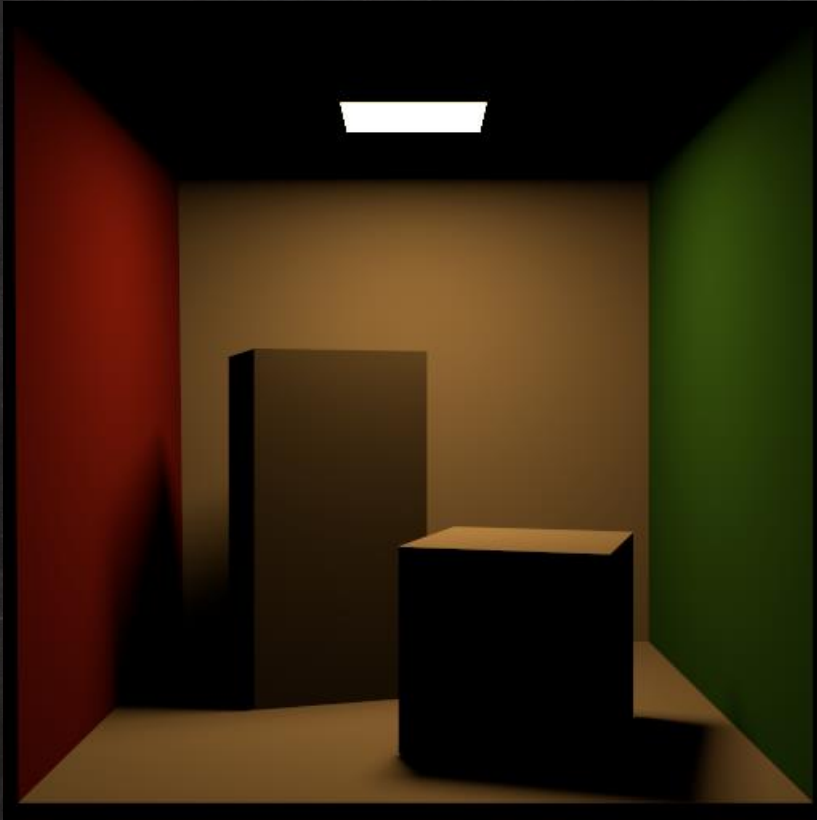
# Basic Concepts

# Where Does Light Come From?

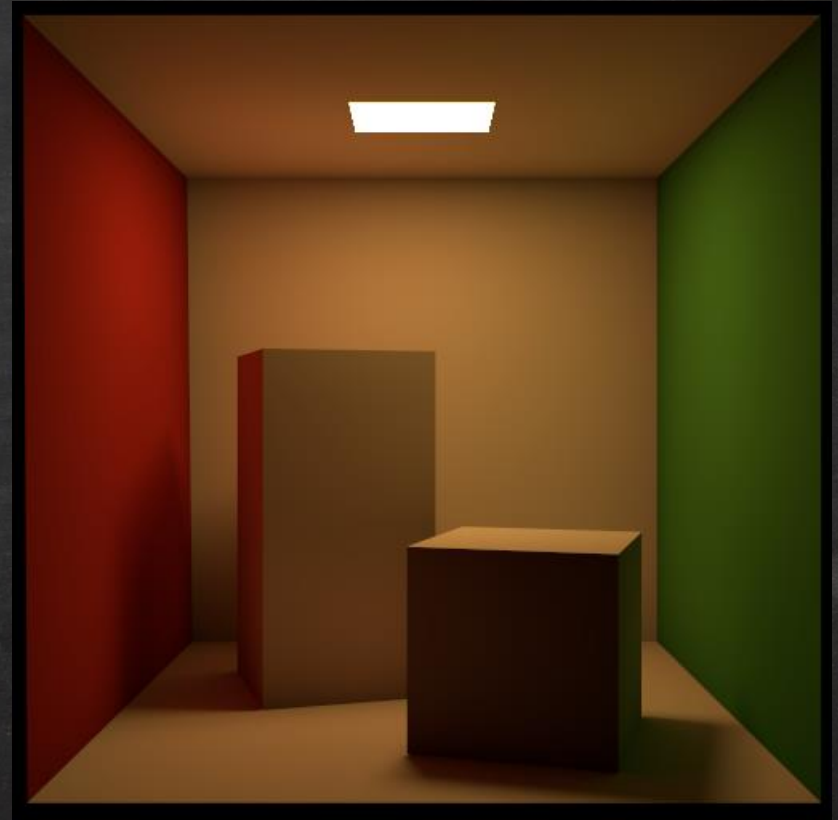




Global = Direct + **Indirect** Lighting

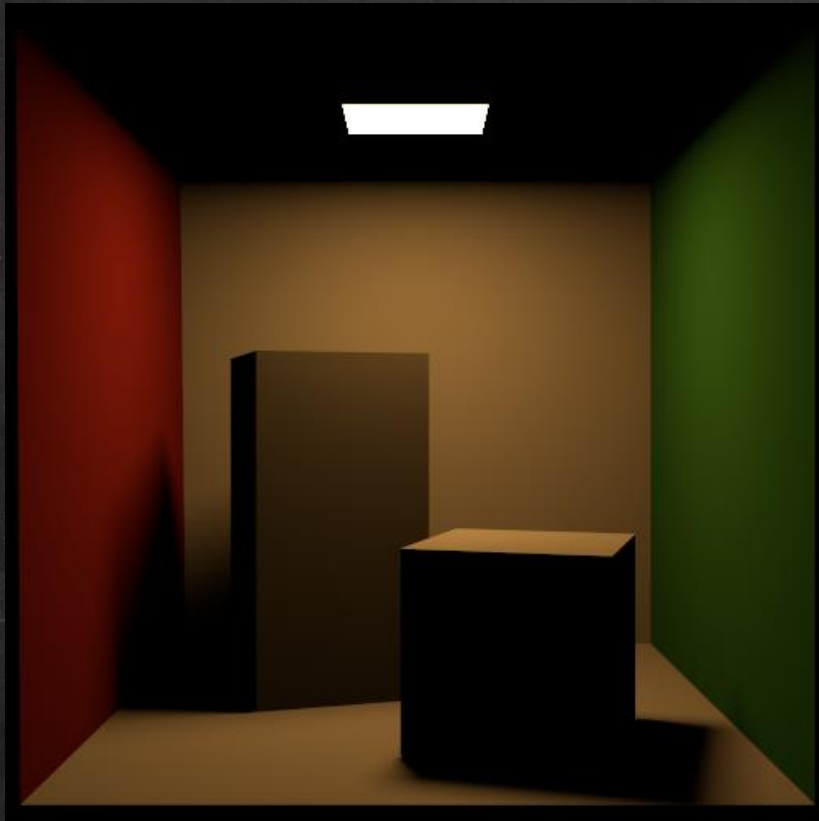


Direct Illumination

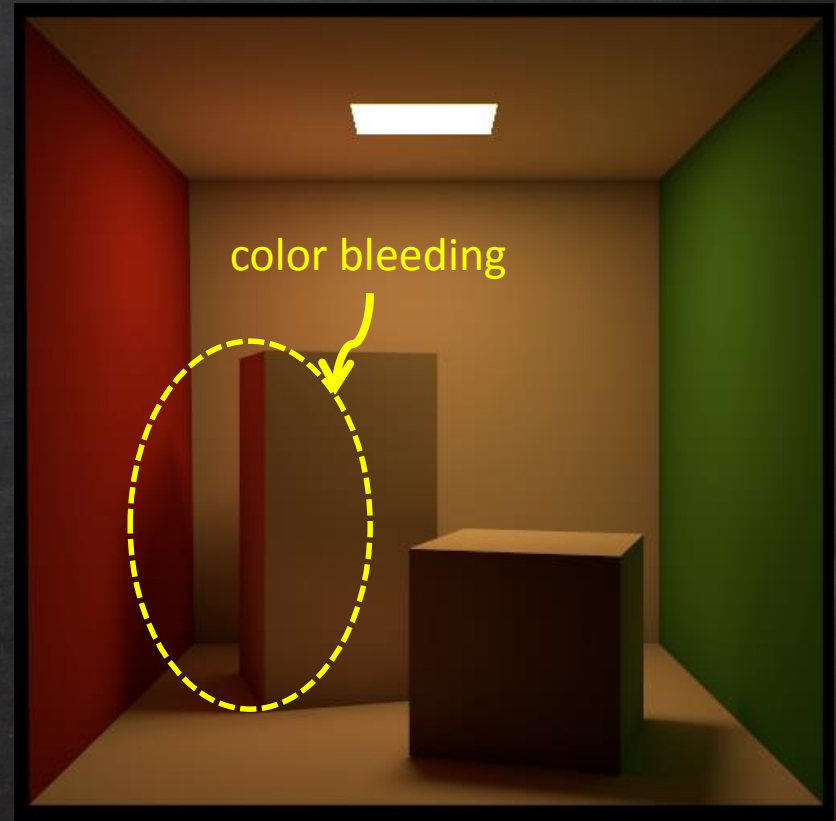


Global Illumination

Global = Direct + **Indirect** Lighting



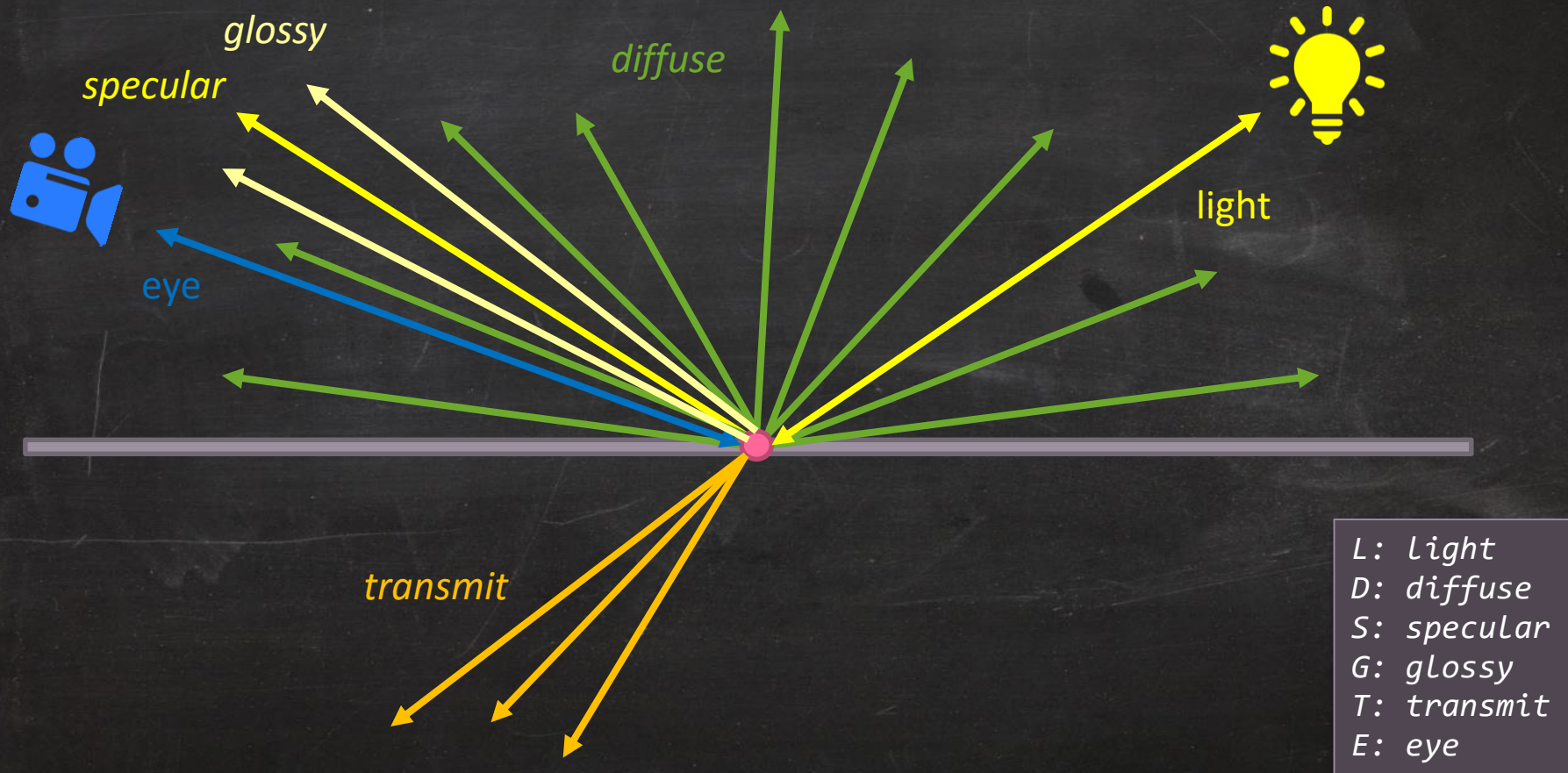
Direct Illumination



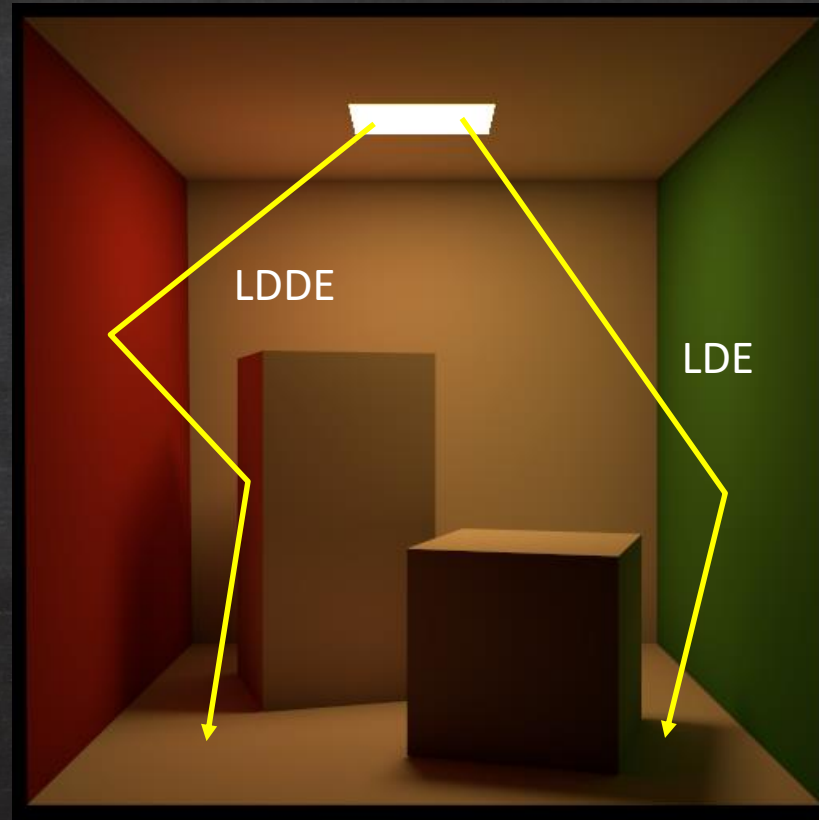
Global Illumination



# Light Path Expression



# Light Path Expression (Cont'd)



# Radiometry

- Irradiance  $E = \frac{d\Phi}{dA}$   
*pre area incoming flux at a surface*
- Radiance  $L = \frac{d^2\Phi}{d\omega dA^\perp} = \frac{d^2\Phi}{d\omega dA \cos \theta}$   
*flux per solidangle per projected area*

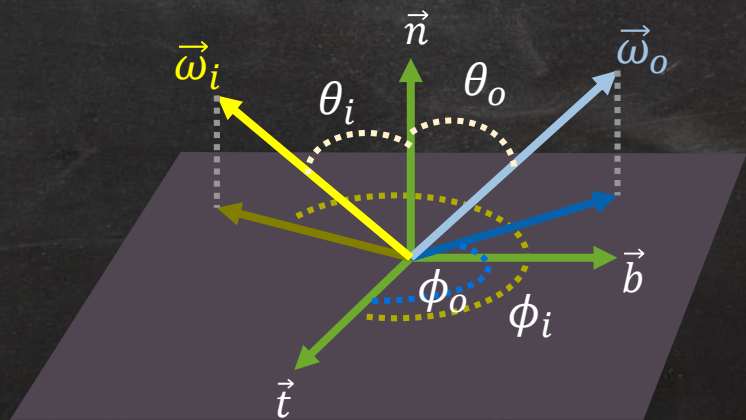
$$L \cos \theta = \frac{d^2\Phi}{dA d\omega} = \frac{dE}{d\omega} \Rightarrow L \cos \theta d\omega = dE$$



## BRDF Definition

spending  
income

$$f(\vec{\omega}_i, \vec{\omega}_o) = \frac{\overset{\text{outgoing radiance}}{dL_r(\vec{\omega}_o)}}{\underset{\text{incoming irradiance}}{dE_i(\vec{\omega}_i)}} = \frac{dL_r(\vec{\omega}_o)}{L_i(\vec{\omega}_i) \cos \theta_i d\omega_i}$$



# Compute $L_r(\vec{\omega}_o)$ from BRDF (temp)



$$f(\vec{\omega}_i, \vec{\omega}_o) = \frac{dL_r(\vec{\omega}_o)}{dE_i(\vec{\omega}_i)} = \frac{dL_r(\vec{\omega}_o)}{L_i(\vec{\omega}_i)(\vec{\omega}_i \cdot \vec{n})d\vec{\omega}_i}$$

$$L_i(\vec{\omega}_i)f(\vec{\omega}_i, \vec{\omega}_o)(\vec{\omega}_i \cdot \vec{n}) = L_i(\vec{\omega}_i) \frac{dL_r(\vec{\omega}_o)}{L_i(\vec{\omega}_i)(\vec{\omega}_i \cdot \vec{n})d\vec{\omega}_i} (\vec{\omega}_i \cdot \vec{n}) = \frac{dL_r(\vec{\omega}_o)}{d\vec{\omega}_i}$$

$$\int_{\Omega} \frac{dL_r(\vec{\omega}_o)}{d\vec{\omega}_i} d\vec{\omega}_i = L_r(\vec{\omega}_o)$$

hemisphere

reflected radiance

# ★ Render Equation

$$\begin{aligned}L_o(x, \vec{\omega}_o) &= L_e(x, \vec{\omega}_o) + \int_{\Omega} L_i(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n}) d\vec{\omega}_i \\ &= L_e(x, \vec{\omega}_o) + L_r(x, \vec{\omega}_o)\end{aligned}$$

emission

reflection



# ★ Render Equation

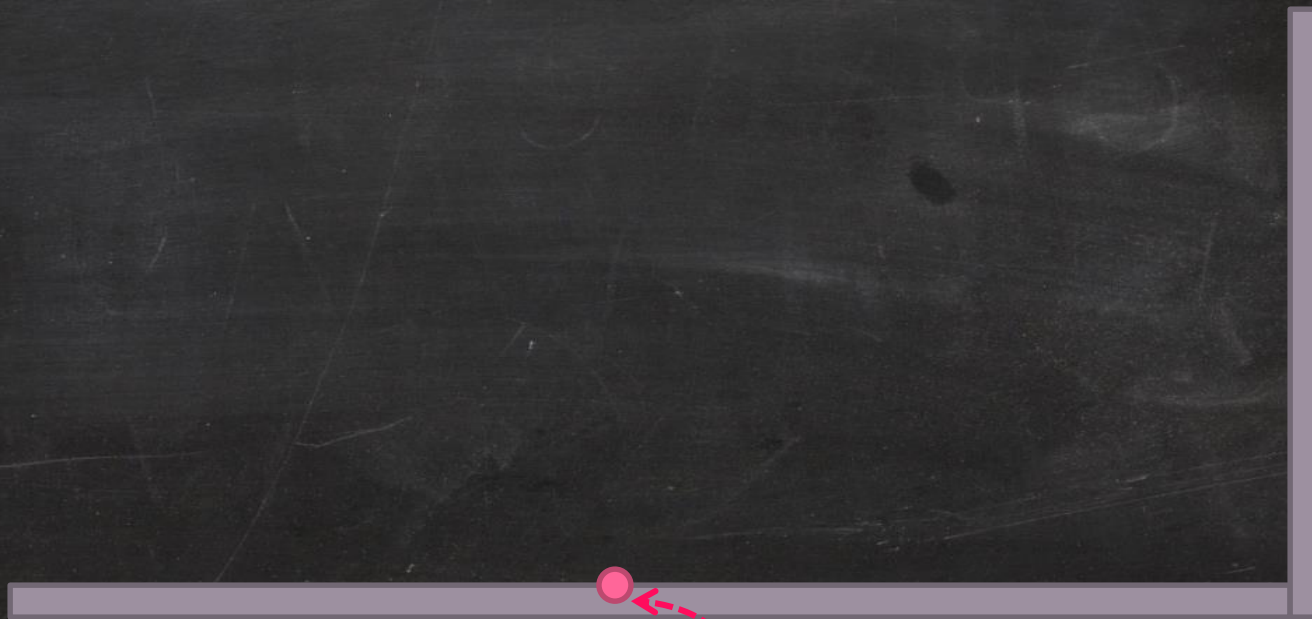
*Oops! There is another **render equation** nested inside!!*

$$L_o(x, \vec{\omega}_o) = L_e(x, \vec{\omega}_o) + \int_{\Omega} L_i(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n}) d\vec{\omega}_i$$
$$= L_e(x, \vec{\omega}_o) + L_r(x, \vec{\omega}_o)$$

emission

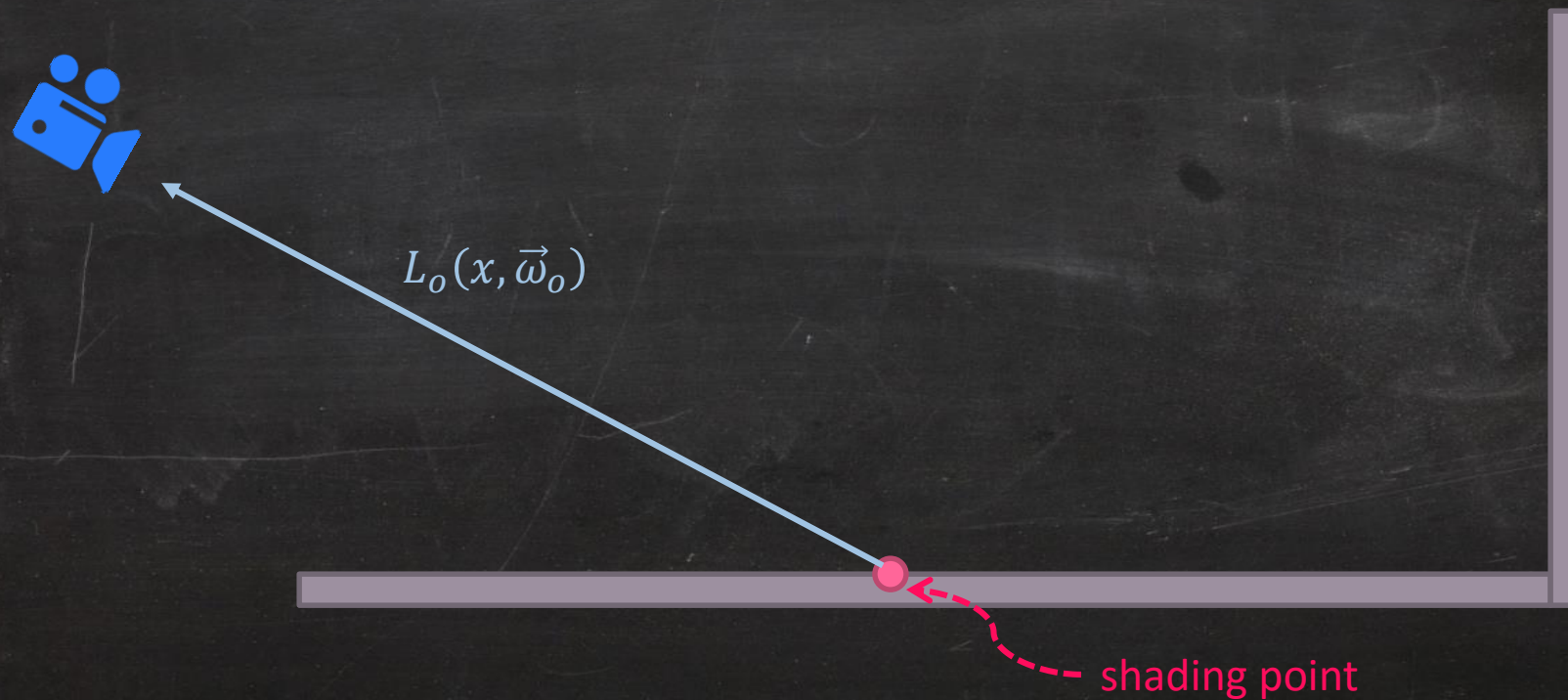
reflection

# Recursive Ray Tracing



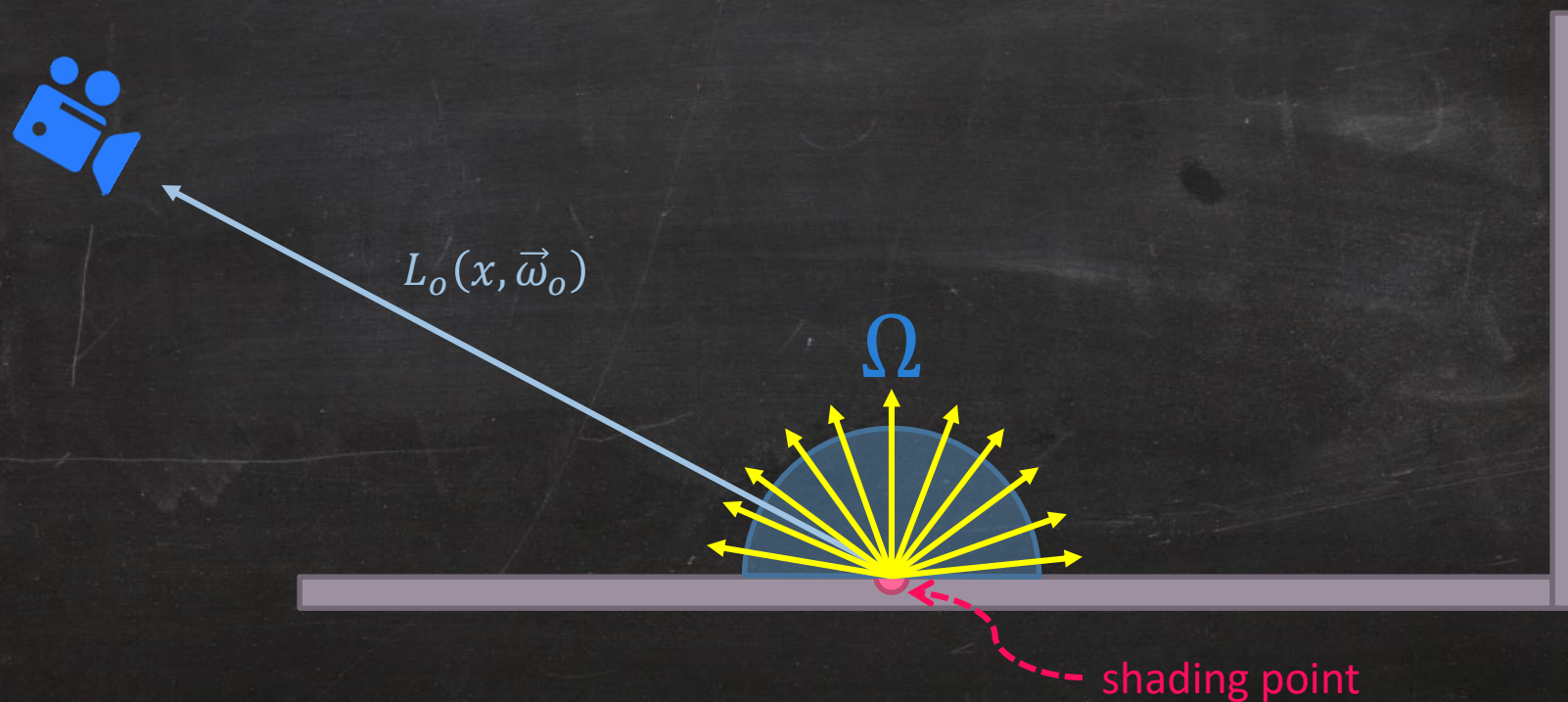
shading point

# Recursive Ray Tracing

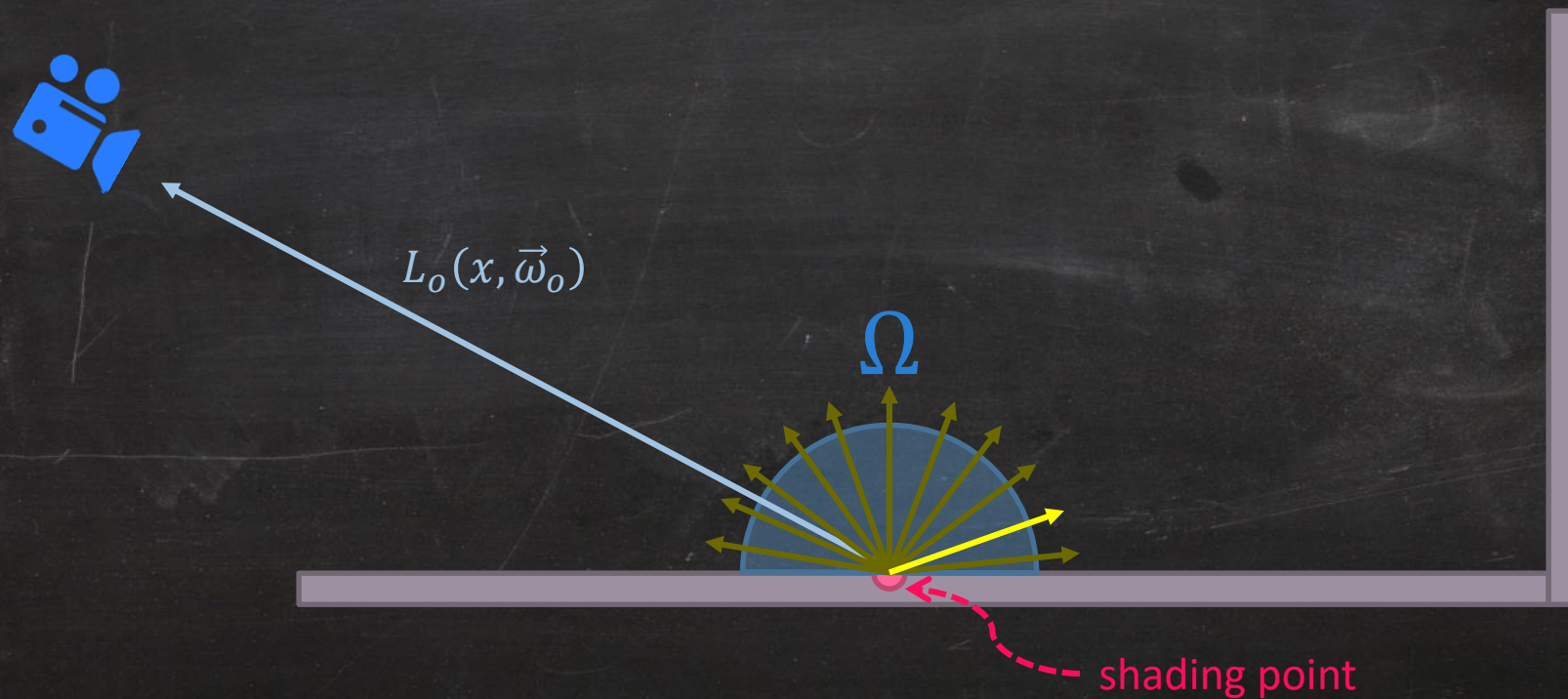




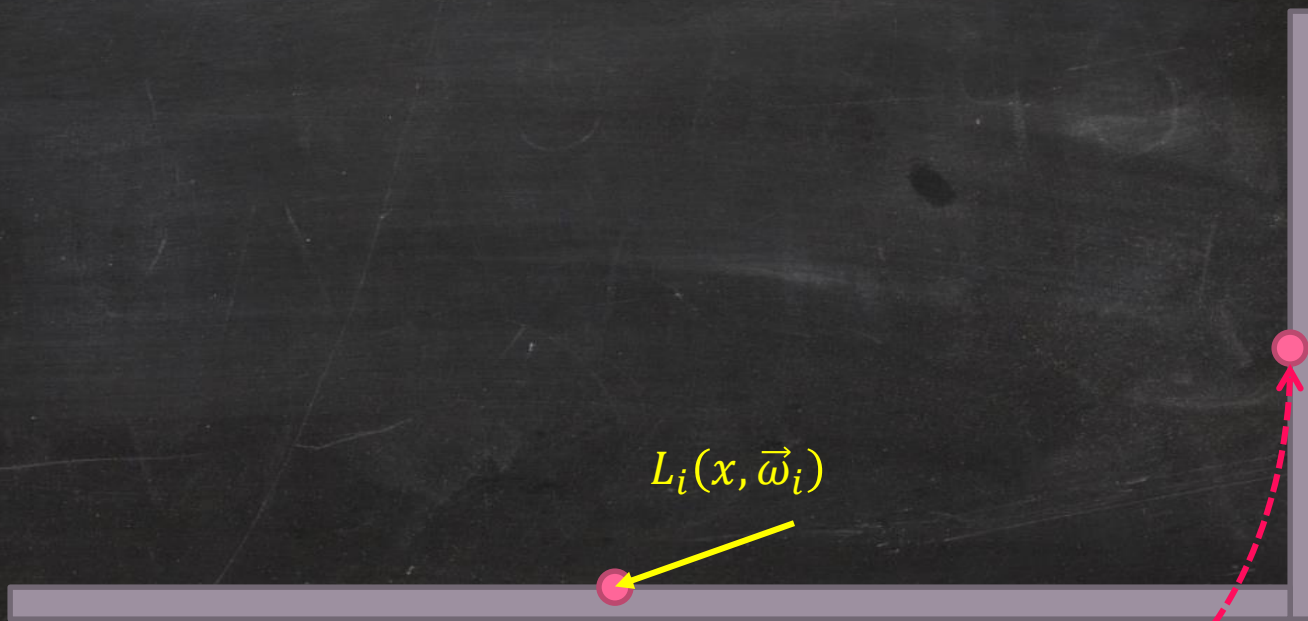
# Recursive Ray Tracing



# Recursive Ray Tracing



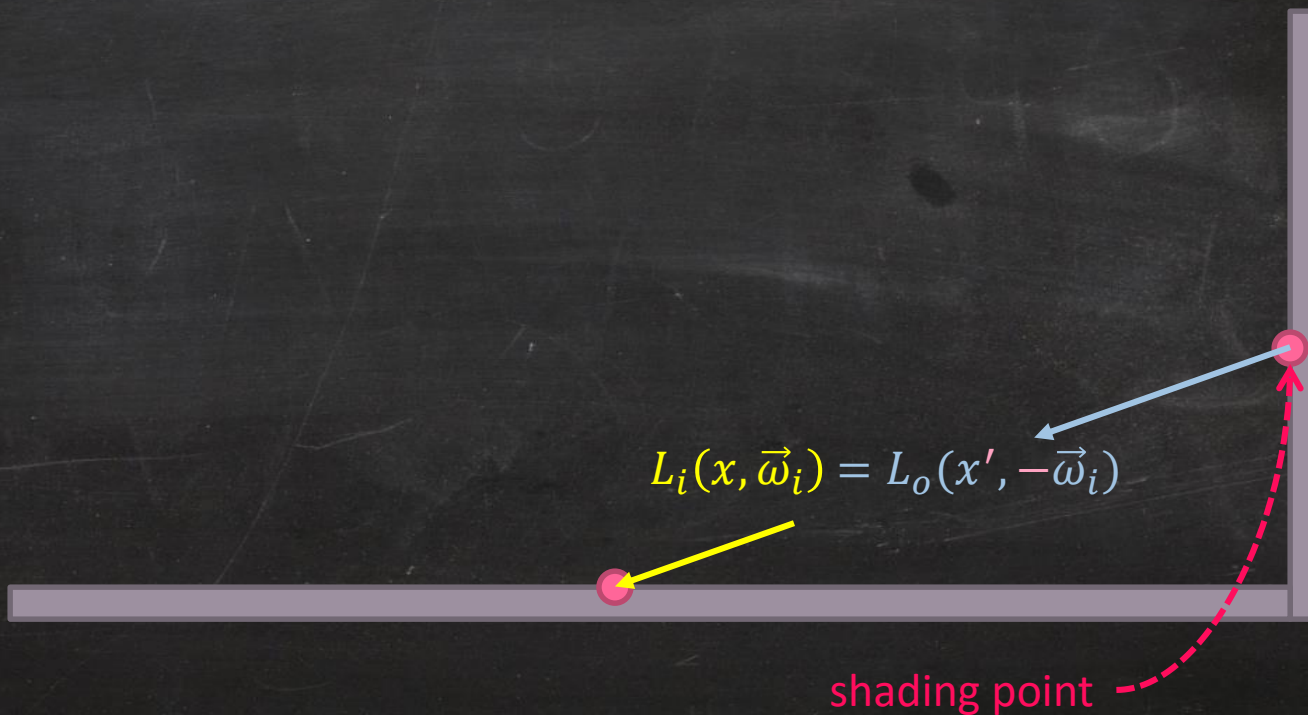
# Recursive Ray Tracing



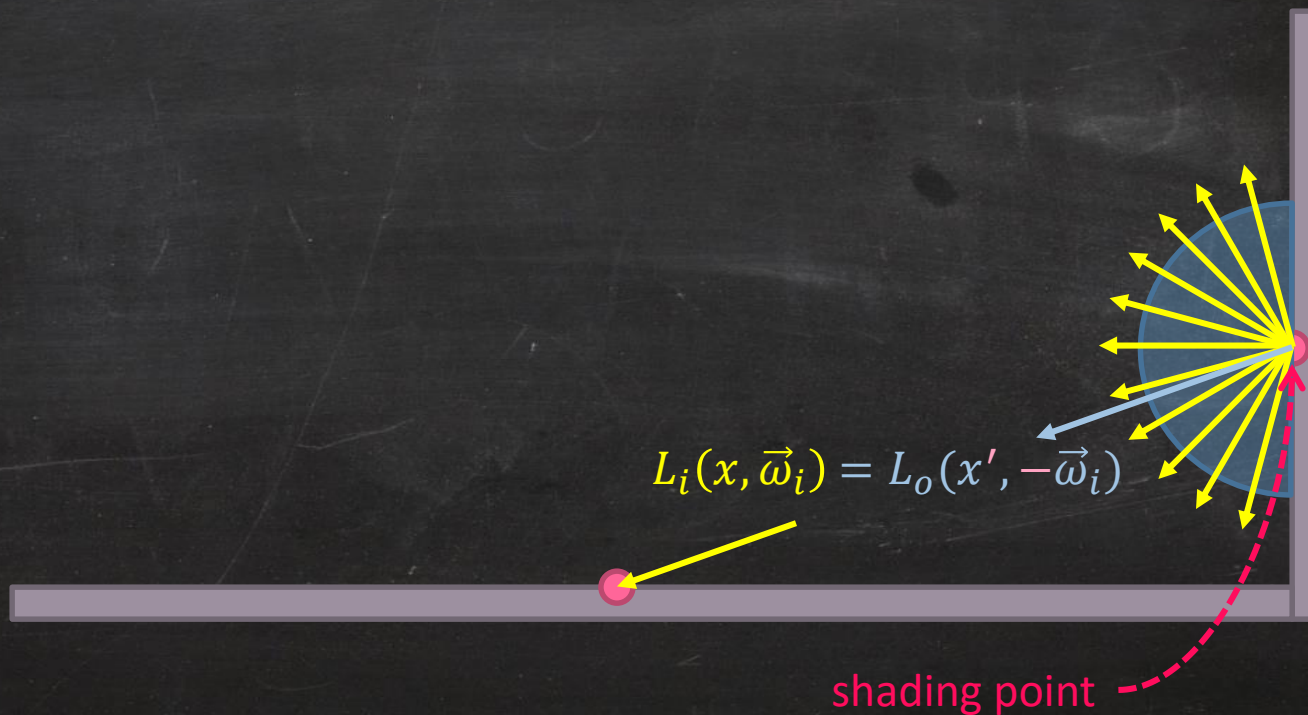
shading point



# Recursive Ray Tracing



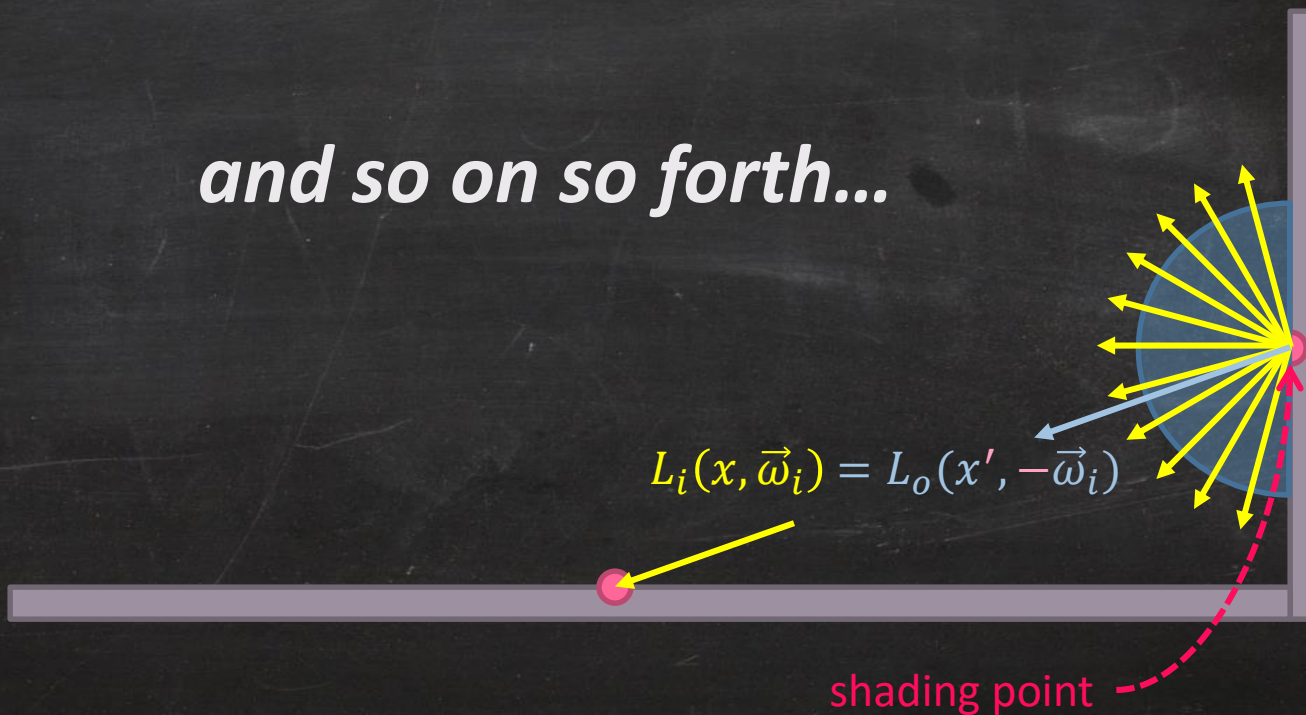
# Recursive Ray Tracing



# Recursive Ray Tracing



*and so on so forth...*





# Primary Visibility

## Rasterization

- Surface to eye
- Visibility via depth buffer



## Ray Tracing

- Eye to surface
- Visibility via ray casting



# Ray-Casting

- Find the nearest intersection from a ray
- Computed with different geometry representations
  - Explicit
    - Triangular meshes
    - Bezier curves for hair/fur
  - Implicit
    - Volume data (voxels)
    - Point cloud

# Acceleration Structures for Ray-Casting



# Ray-Casting Computation

```
for each ray in each pixel:  
  for each geometry primitive in the scene:  
    if intersect(ray, primitive):  
      return closest point
```

# Ray-Casting Computation

```
for each ray in each pixel:  
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```

$O(N)$

spatial coherence

$O(\log N)$

# Spatial Coherence

- Geometry primitives only occupy a small portion of the ambient space
- Primitives can be ordered by their spatial locations
- A location in space is associated with a limited number of primitives



*Then, how should we do ...*



***Divide & Conquer!***



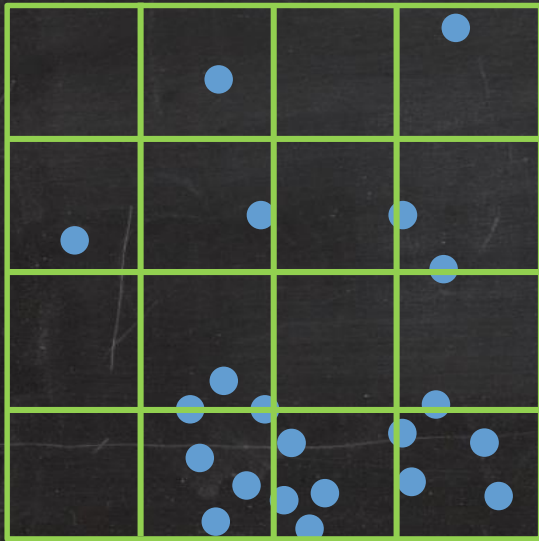
# Acceleration Structures

- Uniform grids
- Quadtree/Octree
- k-D tree
- BSP (Binary Space Partitioning) tree
- Bounding volume hierarchy (BVH)

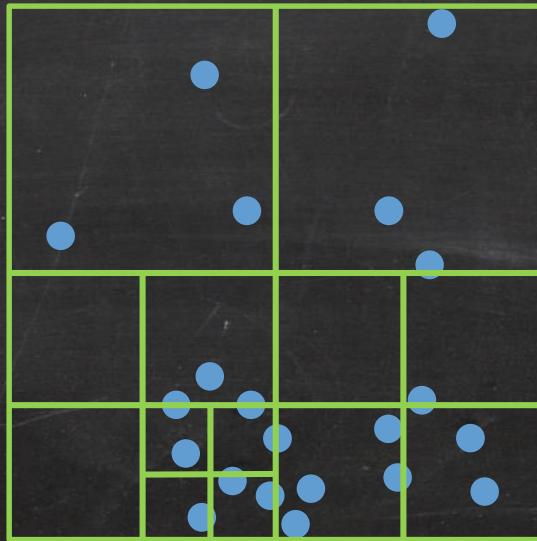


# Spatial Partition

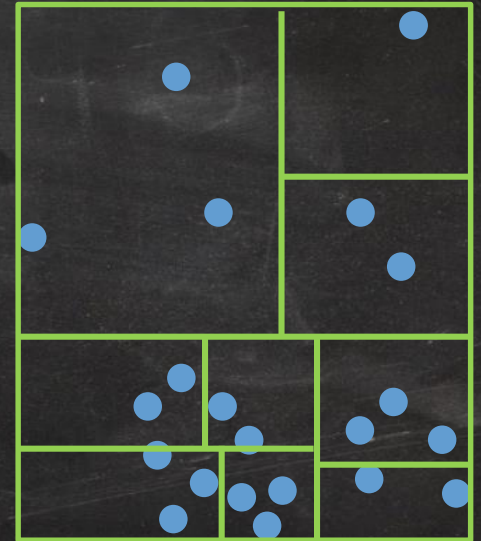
Uniform Grids



Quad Tree

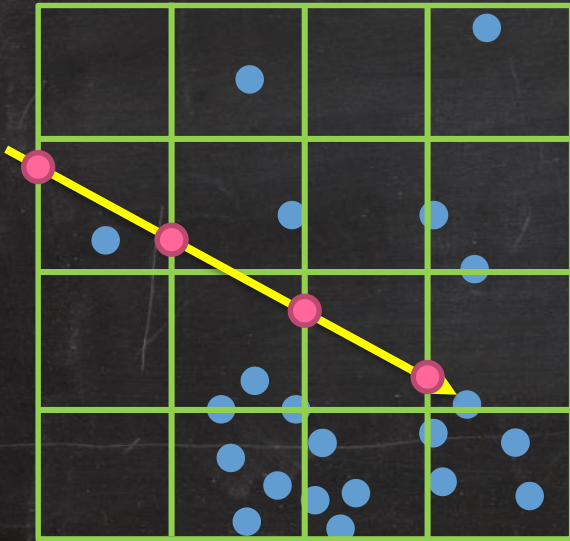


k-D Tree

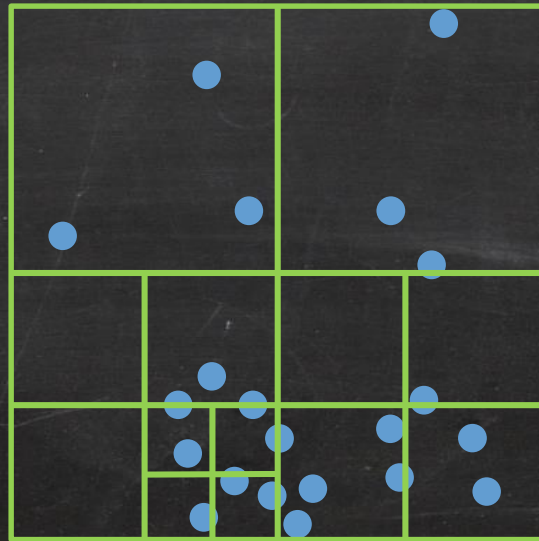


# Spatial Partition

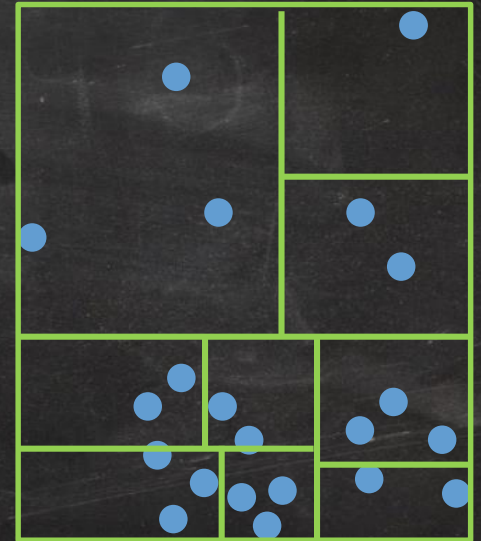
Uniform Grids



Quad Tree

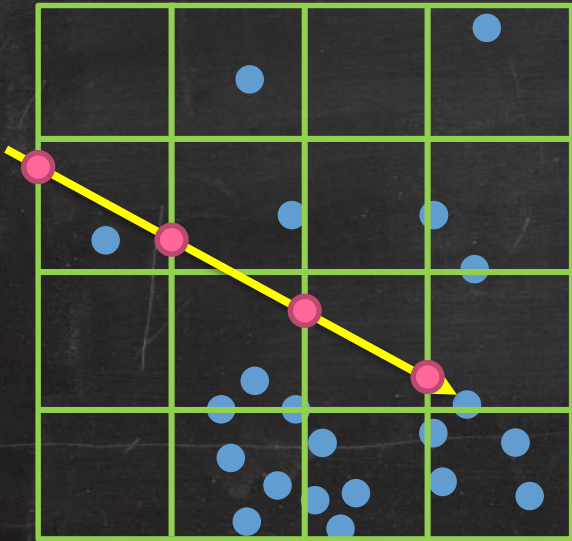


k-D Tree

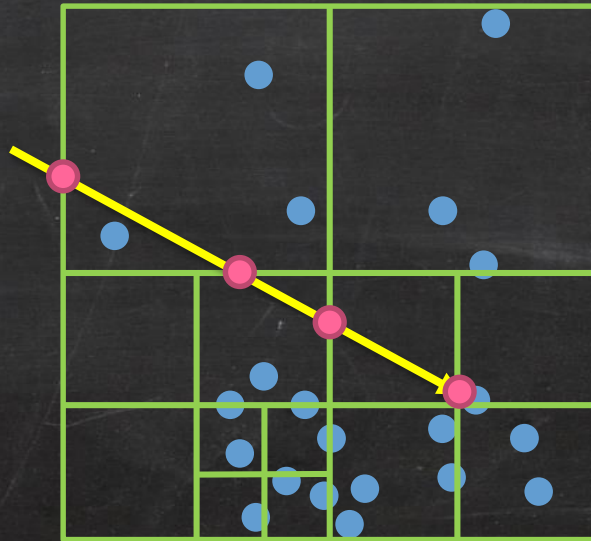


# Spatial Partition

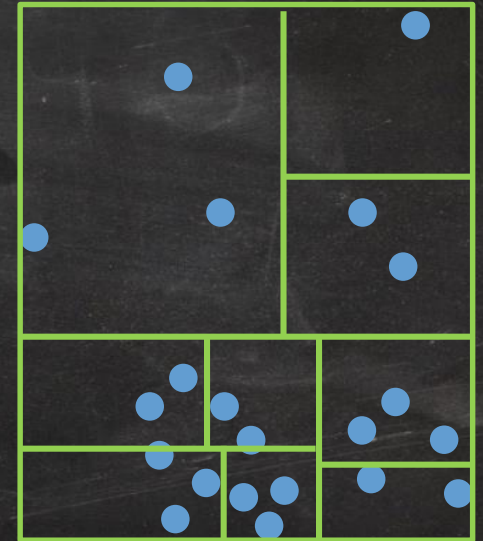
Uniform Grids



Quad Tree



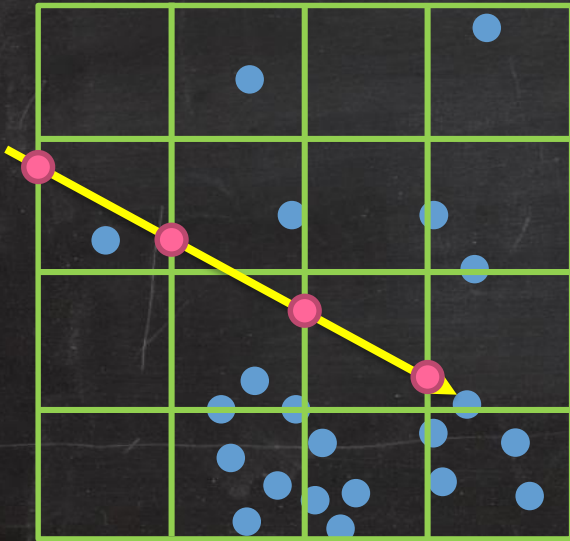
k-D Tree



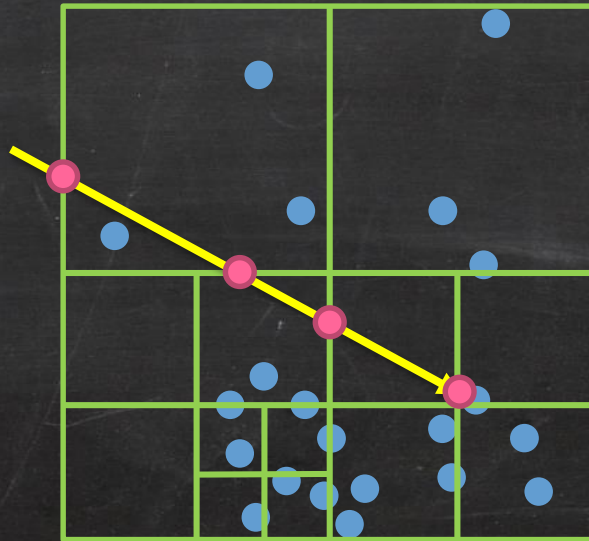


# Spatial Partition

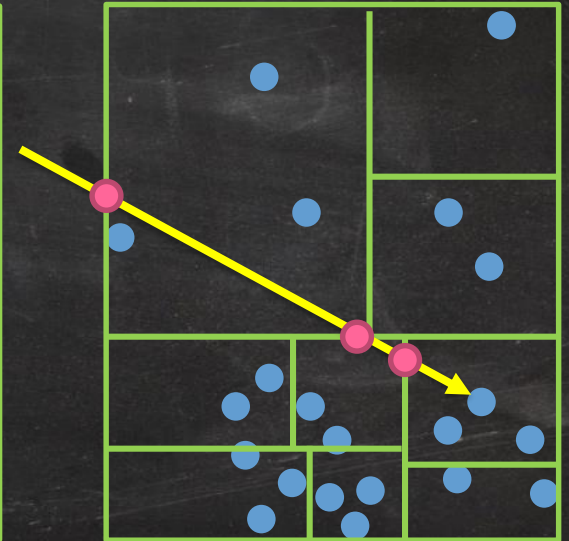
Uniform Grids



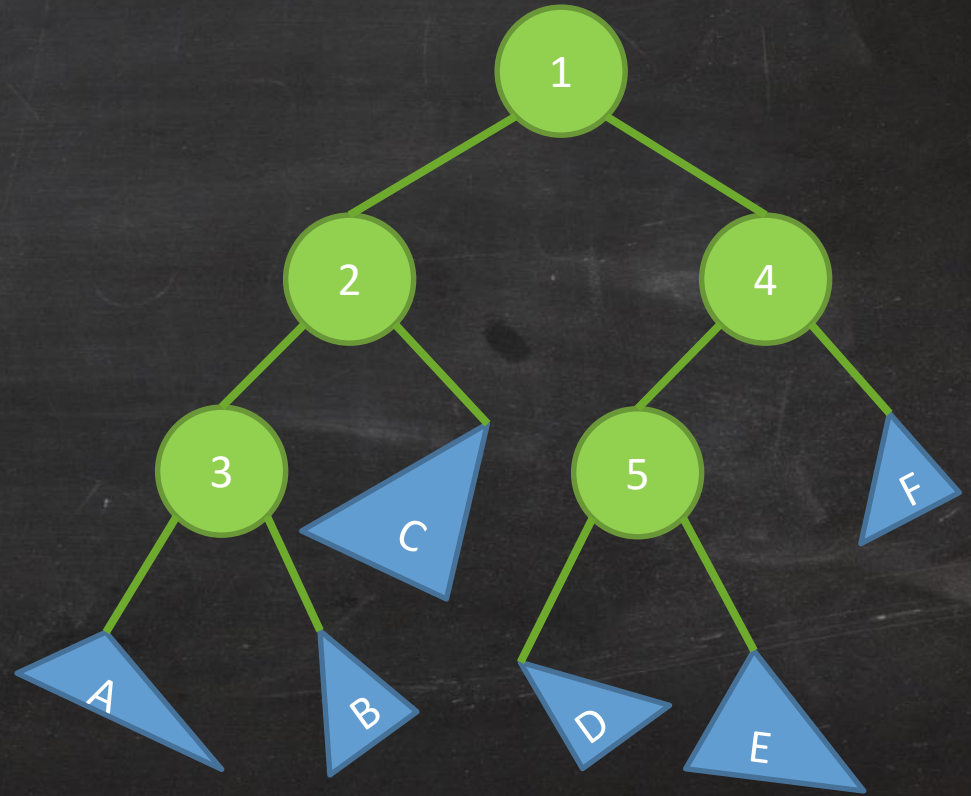
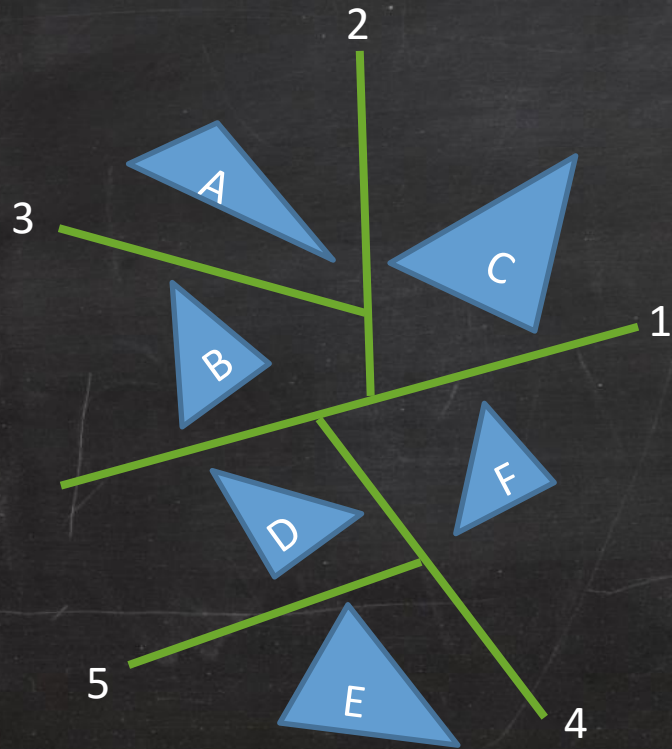
Quad Tree



k-D Tree



# Binary Space Partitioning Tree



# Types of Boundary Volumes



AABB



sphere



k-DOP



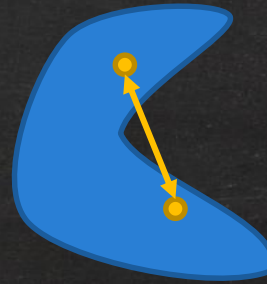
OBB



convex hull



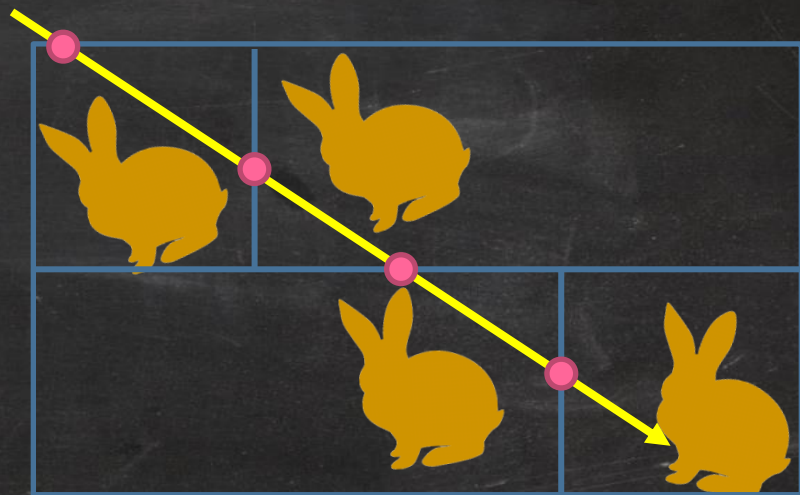
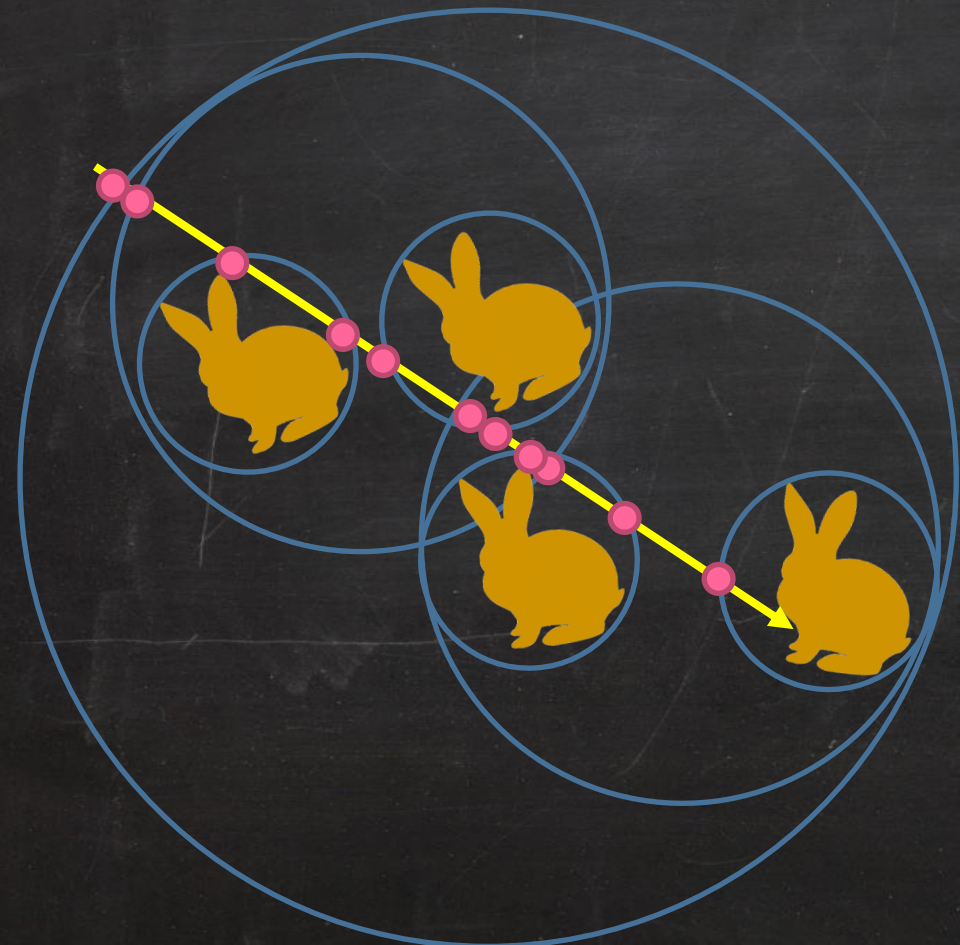
convex



concave

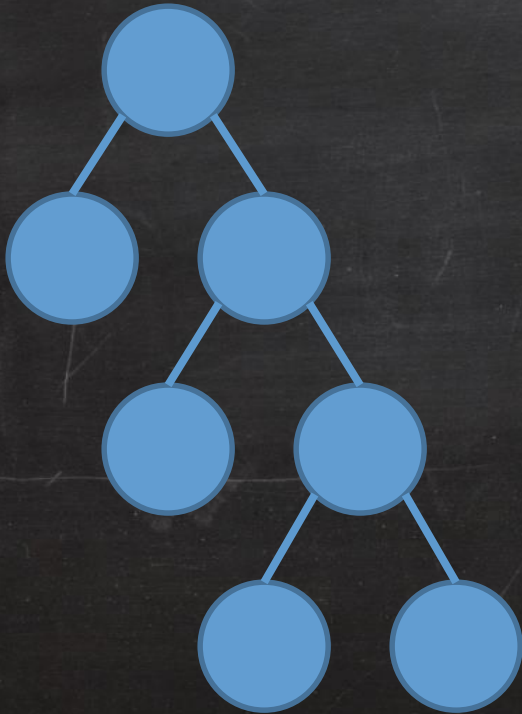


# Hierarchy Traversal

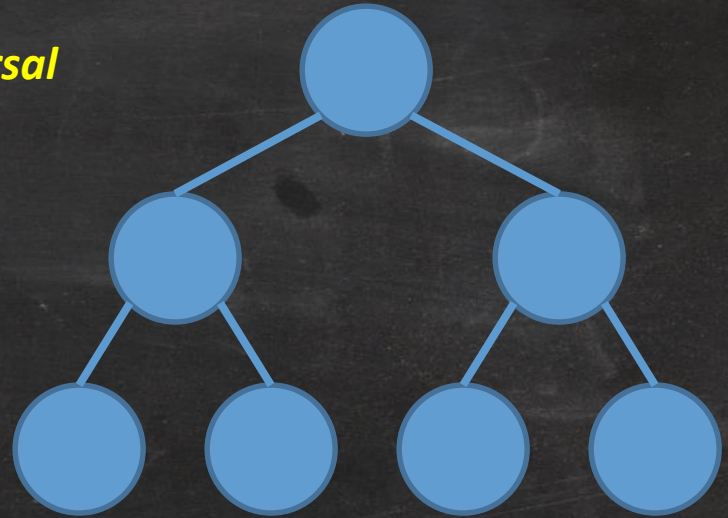


# Balance = Query Performance

Imbalanced



Balanced



*Depth of Traversal*



# Balance = Query Performance

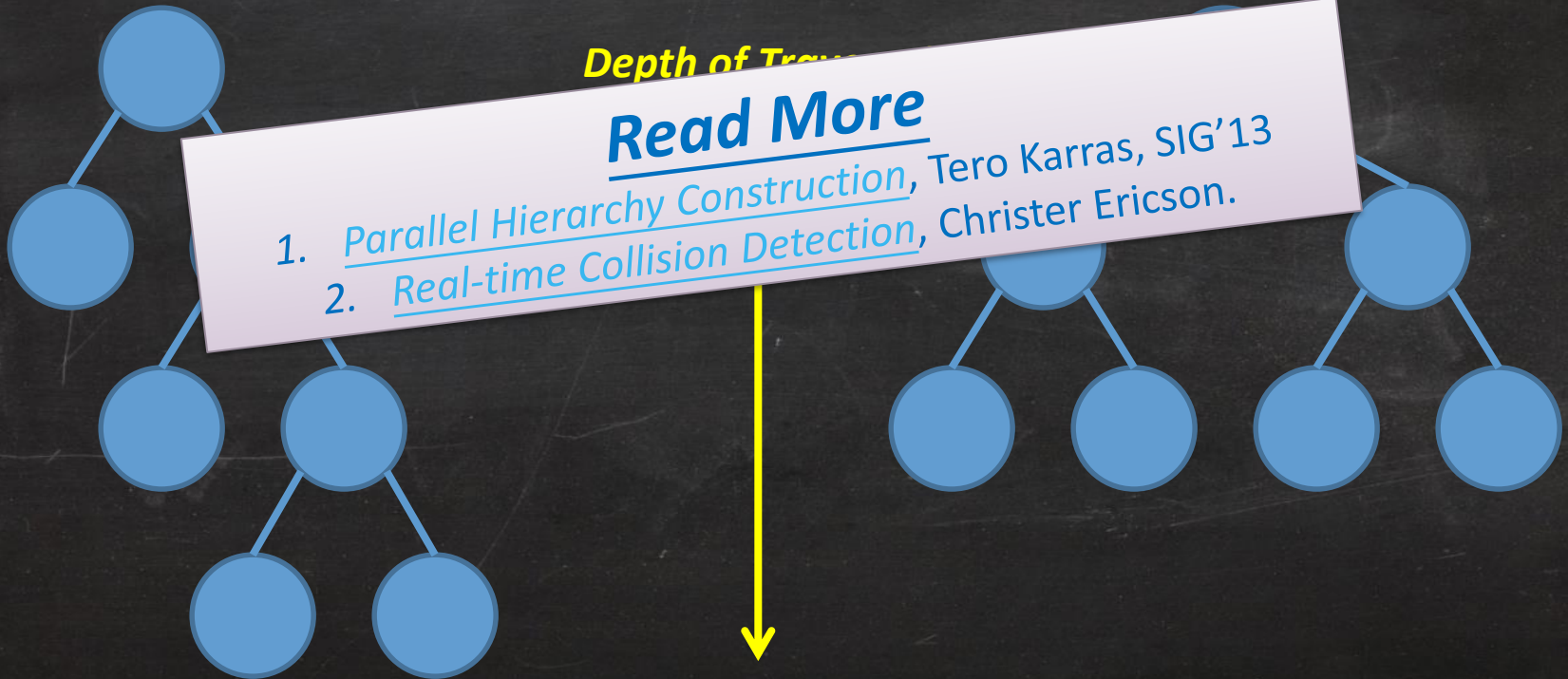
Imbalanced

Balanced

Depth of Tree

Read More

1. Parallel Hierarchy Construction, Tero Karras, SIG'13
2. Real-time Collision Detection, Christer Ericson.





# Ray-Object Intersection



## Object/Object Intersection

Last changed: February 19, 2016

This page gives a grid of intersection routines for various popular objects, pointing to resources in books and on the web. For a unified static and dynamic object intersection and distance library (non-commercial use only, though), see the [TGS collis system](#). The most comprehensive books on the subject are *Geometric Tools for Computer Graphics* (GTGC) and *Real-Time Collision Detection* (RTCD); the former is all-encompassing, the latter more approachable and focused.

Guide to source abbreviations:

- **3DG** - *3D Games: Real-time Rendering and Software Technology*, Alan Watt and Fabio Policarpo, Addison-Wesley, 2001.
- **GPG** - *Game Programming Gems*, ed. Mark DeLoura, Charles River Media, 2000.
- **GTGC** - *Geometric Tools for Computer Graphics*, Philip J. Schneider and David H. Eberly, Morgan Kaufmann Publishers, 2002. Good, comprehensive book on this topic.
- **Gems** - *The Graphics Gems series*. See the book's website for individual book links and code.
- **GTweb** - Geometric Tools, Dave Eberly's online computer graphics related software repository. His book *3D Game Engine Design* also covers these, in a readable format, as well as many other [object/object intersection tests](#).
- **IRT** - *An Introduction to Ray Tracing*, ed. Andrew Glassner, Academic Press, 1989.
- **JCGT** - *The Journal of Computer Graphics Techniques*.
- **jgt** - *journal of graphics tools*. A partial code repository is available.
- **RTCD** - *Real-Time Collision Detection*, by Christer Ericson, Morgan Kaufmann Publishers, 2004.
- **RTR** - *Real-Time Rendering, Third Edition*, by Tomas Möller, Eric Haines, and Naty Hoffman, A.K. Peters Ltd., 2008.
- **RTR2** - *Real-Time Rendering, Second Edition*, by Tomas Akenine-Möller and Eric Haines, A.K. Peters Ltd., 2002.
- **SG** - Simple Geometry library, Steve Baker's vector, matrix, and quaternion manipulation library.
- **TGS** - Teikitu Gaming System Collision, Andrew Aye's object/object intersection/distance and sweep/penetration software (non-commercial use only).
- **TVCG** - *IEEE Transactions on Visualization and Computer Graphics*.

Individual article references follow after the table.

## Static Object Intersections

Entries are listed from oldest to newest, so often the *last* entry is the best. This table covers objects not moving; see the next section for dynamic objects.

	ray	plane	sphere	cylinder	cone	triangle	AABB	OBB	frustum	polyhedron
ray	Gems p.304; SG; TGS; RTCD p.198; SoftSurfer; RTR2 p.618; RTR3 p.781	IRT p.50,88; SG; GTGC p.482; TGS; RTCD p.175; SoftSurfer (more)	IRT p.39,91; Gems p.388; Held jgt 2(4); GTweb; 3DG p.16; GTGC p.501; TGS; RTCD p.127,177; RTR2 p.568; RTR3 p.738	IRT p.91; Gems IV p.356; Held jgt 2(4); GTweb; GTGC p.507; TGS; RTCD p.194	IRT p.91; Gems V p.227; Held jgt 2(4); GTweb; GTGC p.512	Möller- Trumbore jgt 2(1): code (mirror), paper draft; IRT p.53,102; Gems IV p.24; Held jgt 2(4); GTweb; 3DG p.17; Möller (mirror); GTGC p.485; TGS; RTCD p.153,184; Løfstedt jgt 10(2): code, paper draft Chirkov jgt 10(3): code; Lagae jgt 10(4): code, paper draft; SoftSurfer; RTR2 p.578; RTR3 p.746; Havel TVCG June 2009; Woop JCGT 2(1)	IRT p.65,104; Gems p.395; Smits; 3DG p.20; Terdiman (optimized Woo); Schroeder; GTGC p.626; Gomez; GTGC p.630; TGS; RTCD p.179; Mahovsly jgt 9(1); Williams jgt 10(1) (code); Eisemann jgt 12(4) (code); RTR2 p.572; RTR3 p.742; Shirley 2016	(IRT p.104; Gems II p.247); GTweb; Gomez; GTGC p.630; TGS; RTCD p.179; RTR2 p.572; RTR3 p.743	(IRT p.104; Gems II p.247)	IRT p.104; Gems II p.247; GTGC p.493; Plats jgt 8(4); RTCD p.198; SoftSurfer

# Practical Issues

- Construction costs in space and time
  - Use float for scalar data instead of double
  - Pointers are costly in x64 platform
    - Might point to incontiguous memory location in heap
    - To save storage, try using int32 or short for indexing
  - Geometry compression?
    - Unit vector quantization
    - Store local position in float, only use double for their transform matrix
- Parallelism and locality are key factors for parallel processing

# Practical Issues

- Construction costs in space and time
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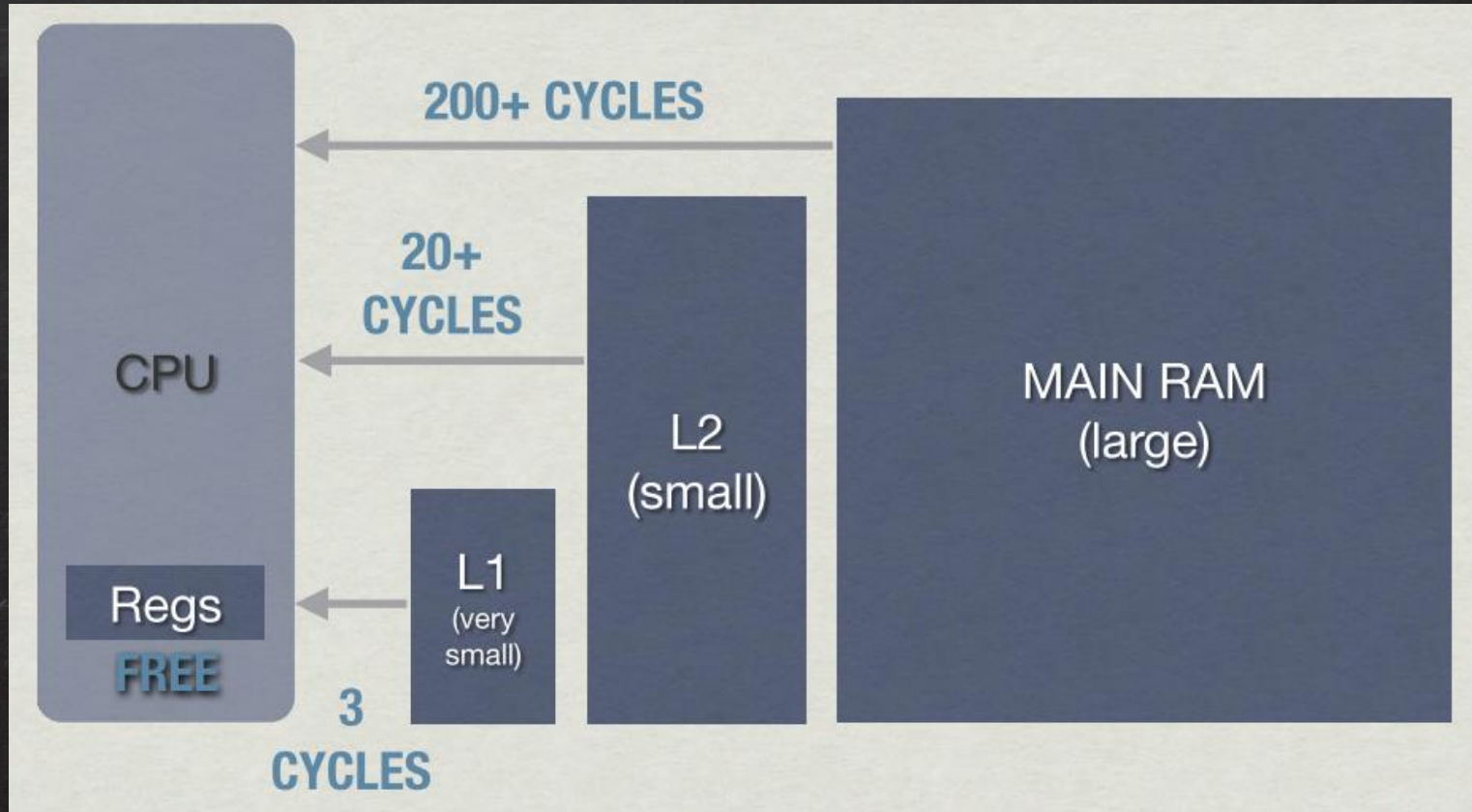
## Read More

1. [A Survey of Efficient Representations](#), Zina H. Cigolle et al., JCGT'14.
2. [Geometry Compression](#), Michael Deering, Computer Graphics '95.

- Store local position in float, only use double for their transform matrix
- Parallelism and locality are key factors for parallel processing

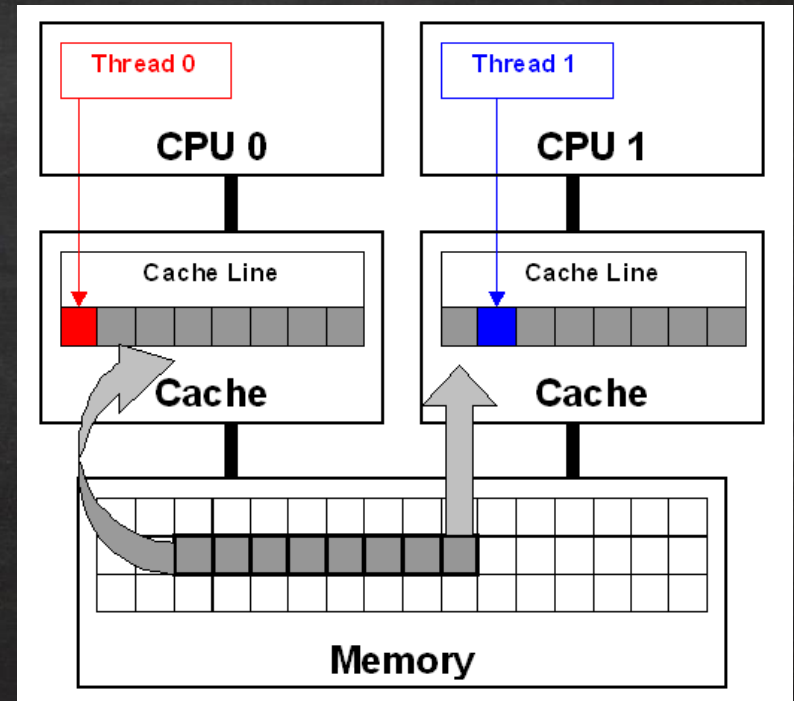


# Memory Caching

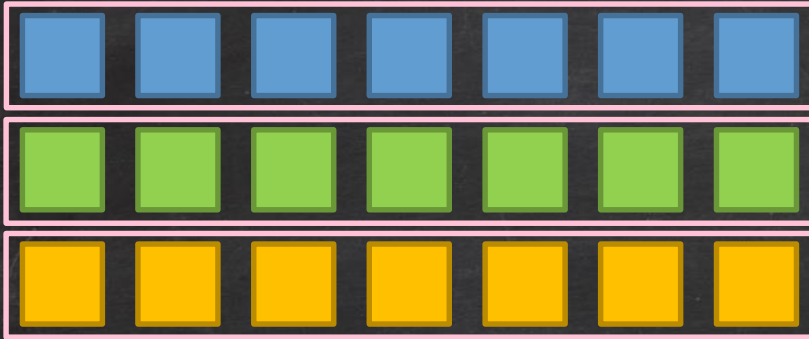


# Cache Line

- The fixed size data block transferred between memory and cache
- Might take hundreds of clocks to move around
- False sharing
  - Different threads access elements which reside in the same cache line



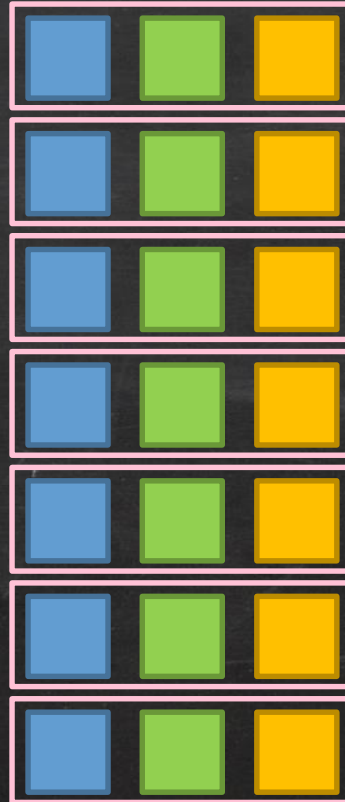
# SOA vs. AOS



## *Structures of Arrays (SOA)*

- Easily aligned cache boundaries
- Easier to utilize SIMD
- Chance for hardware prefetching

## *Array of Structures (AOS)*



- Intuitively match the object abstraction
- Might cause cache alignment problems
- Hard to vectorized



# SOA vs. AOS



## Array of Structures (AOS)



### Read More

1. [CPU Caches and Why You Care](#), Scott Meyers.
2. [Cache Aware Components](#), Randy Gaul.

### Structures of Arrays (SOA)

- Easily aligned cache boundaries
- Easier to utilize SIMD
- Chance for hardware prefetching

- Intuitively match the object abstraction
- Use cache friendly problems
- Vectorized

# Object-Oriented or Data-Oriented Design?

- Abstraction is good for modeling
  - But over-abstraction is harmful for performance
- Memory access pattern is crucial for parallel processing
  - Structure of arrays (SOA) vs. Array of structures (AOS)
  - Hot/cold splitting
- 80/20 principle
  - Optimizing **after profiling!!**
  - Don't optimizing the insignificant parts

# Object-Oriented or Data-Oriented Design?

- Abstraction is good for modeling
  - But over-abstraction is harmful for performance
- Memory access patterns
  - Striding
  - Hoisting
- 80/20 principle
  - Optimizing **after profiling!!**
  - Don't optimizing the insignificant parts

**Read More**

1. [Data Oriented Design](#), Richard Fabian.
2. [Data-Oriented Design and C++](#), Mike Acton, CppCon'14.



# Out-of-Core Algorithms

- What if the data are **too large** to fit the main memory?
  - Conventional algorithm doesn't work!
  - Reduce the times of data reading as many as possible
    - Avoid rewinding all data elements
  - Dice one computation task into several sub-tasks
    - Need to estimate the memory consumption for each sub-task
  - Apply the concept of 'paging'
    - Use memory mapped file during computation