

Global Illumination II

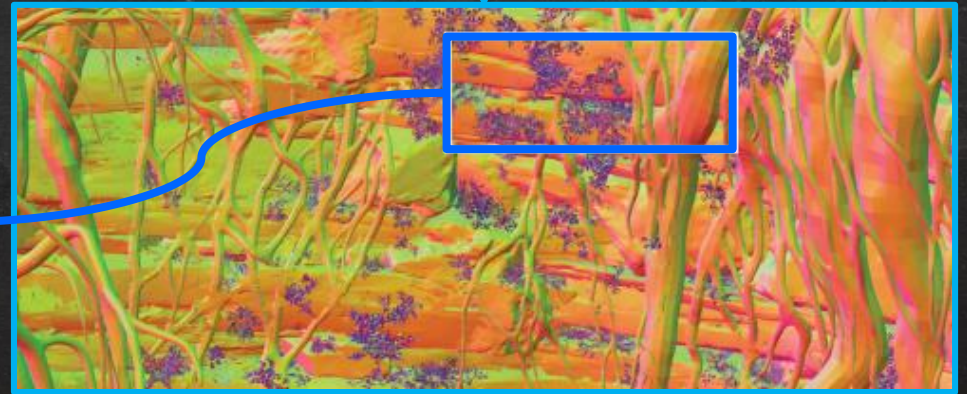
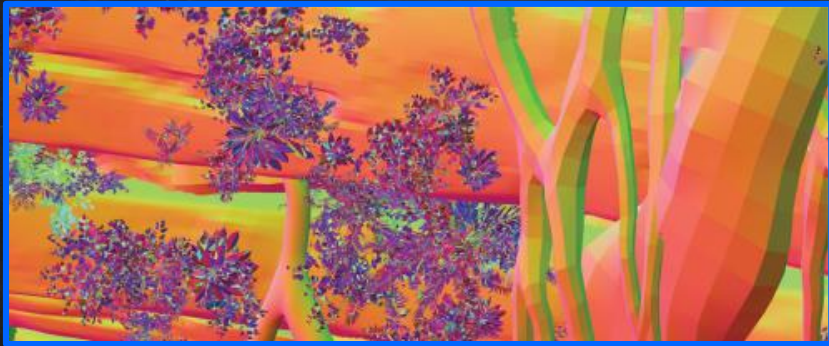
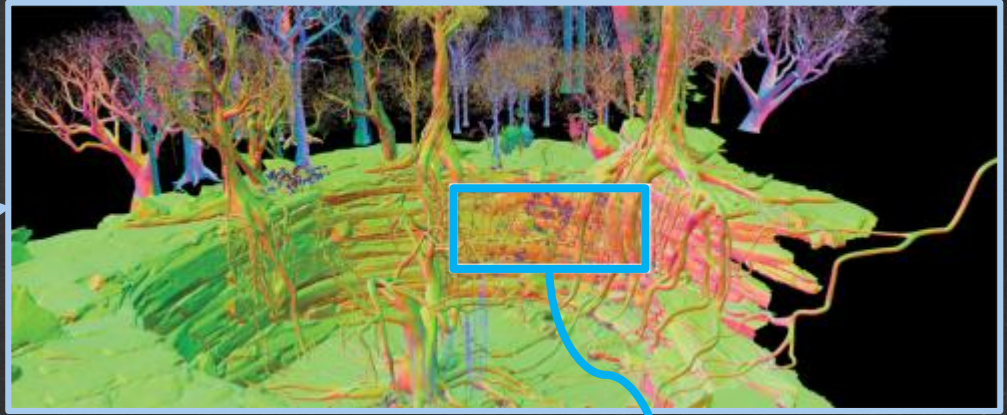
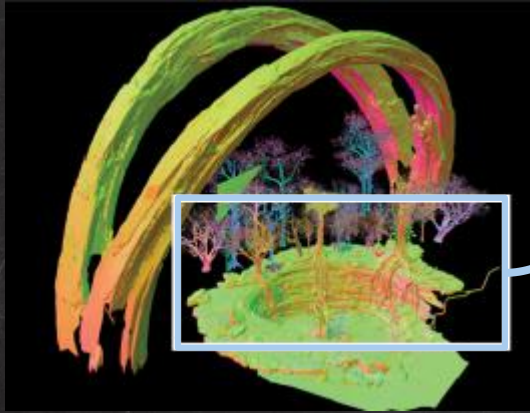
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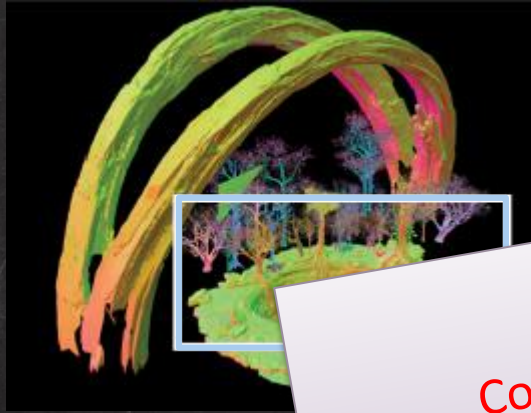
Case Study

PantaRay from NVidia & Weta

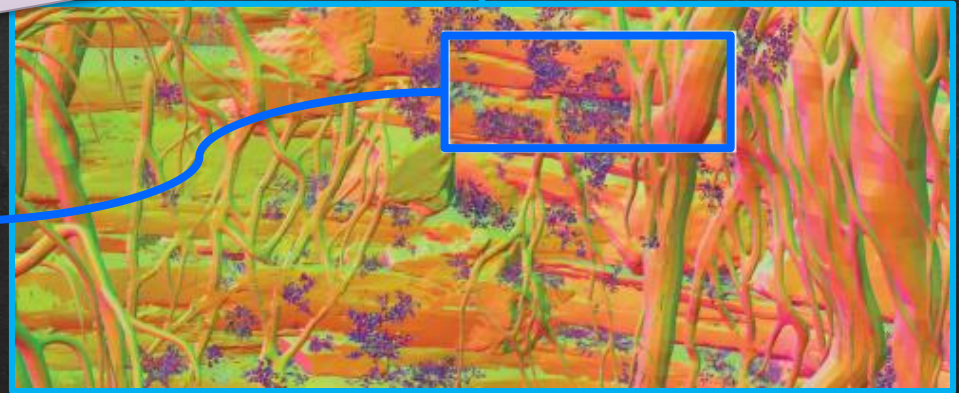
Scenario of PantaRay



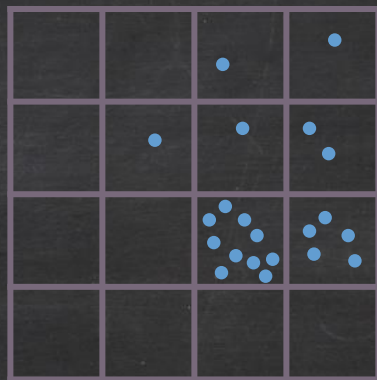
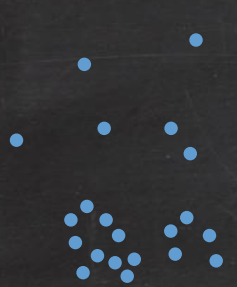
Scenario of PantaRay



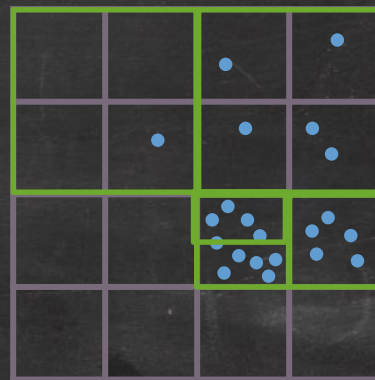
Challenge
Construct acceleration structure from massive dataset that can't fit in main memory!



Case Study: PantaRay



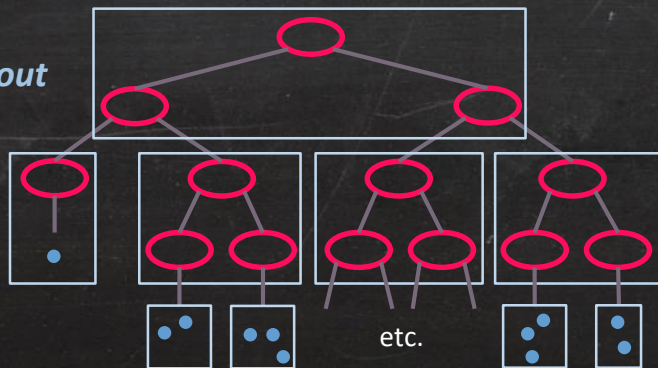
Bucking



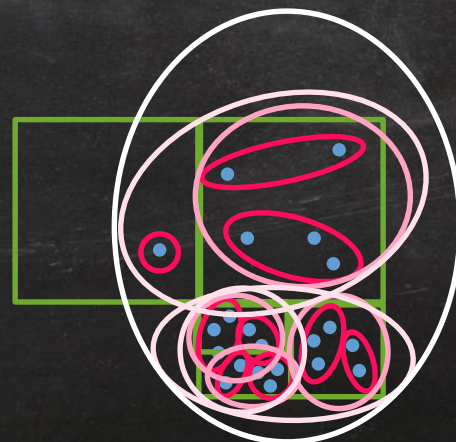
Splitting to chunks (green)



van Emde Boas Layout



Converting to Bricks



BVH construction

Case Study

Hyperion from Disney Animation

Concerns of Production Renderers

- Computation bound or I/O bound?
- Challenges
 - Massive geometry data set
 - Buildings, forest, hair, fur, etc.
 - Large amount of high-resolution textures
- Goals
 - Reduce I/O costs
 - Improve memory access patterns

The Beauty of San Fransokyo



[Video courtesy of Disney Animation.]

City View of San Fransokyo



[Video courtesy of Disney Animation.]

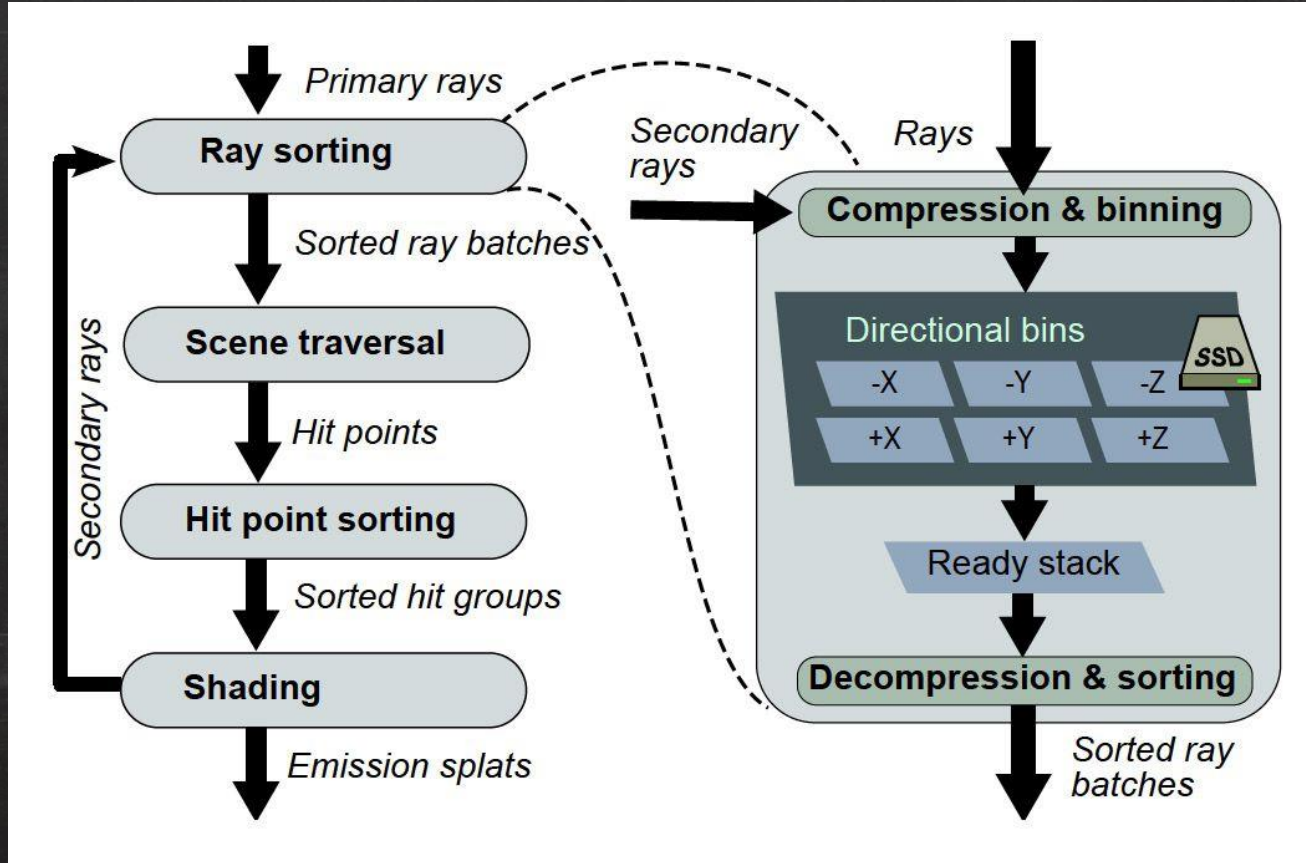
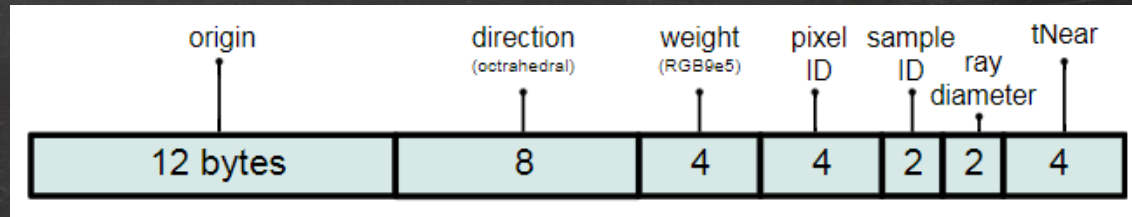
Introduction of Hyperion in Big Hero 6

- Features
 - Uni-directional path tracer (w/o intermediate caches)
 - Physically based rendering
 - Support volumetric rendering and mesh lights, etc.
- Data complexity
 - 83,000 buildings
 - 216,000 street lights

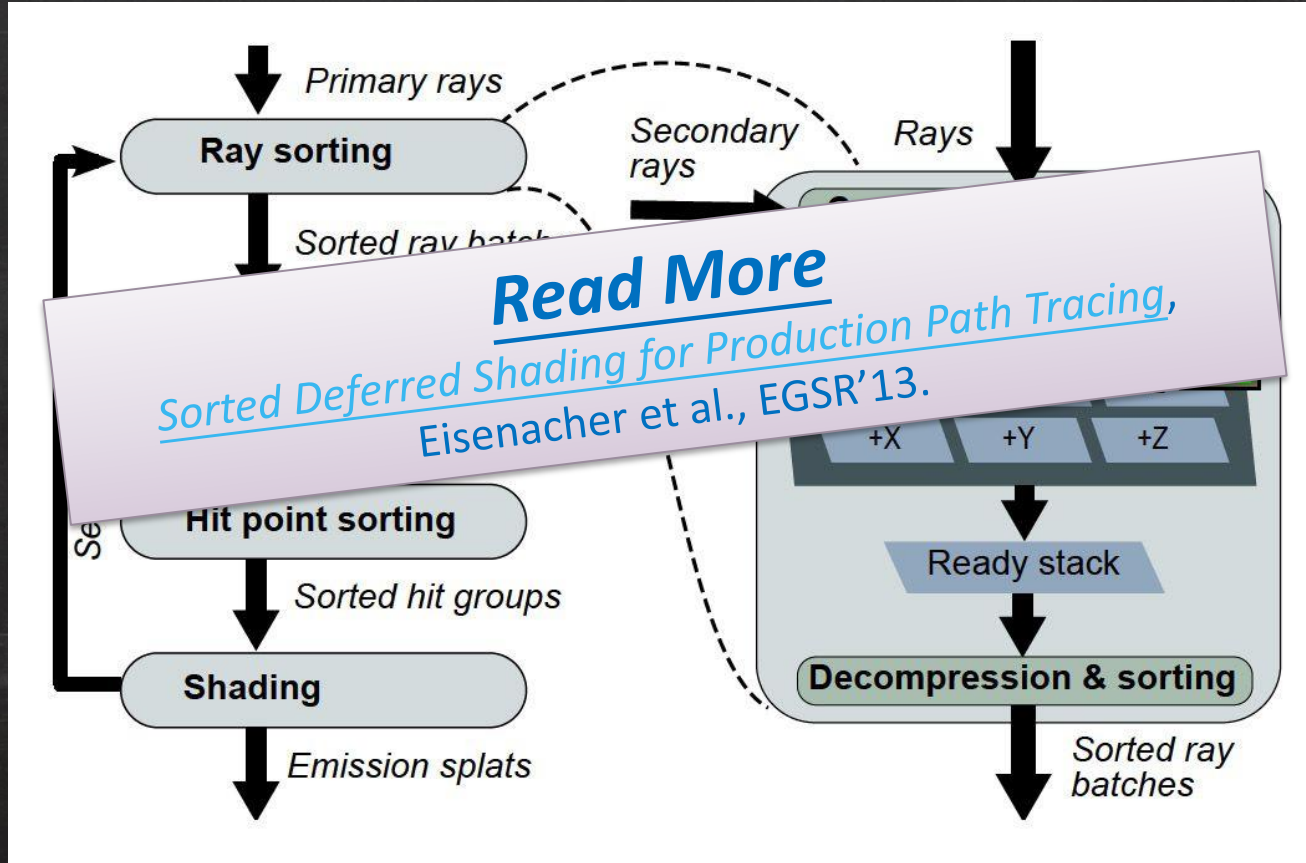
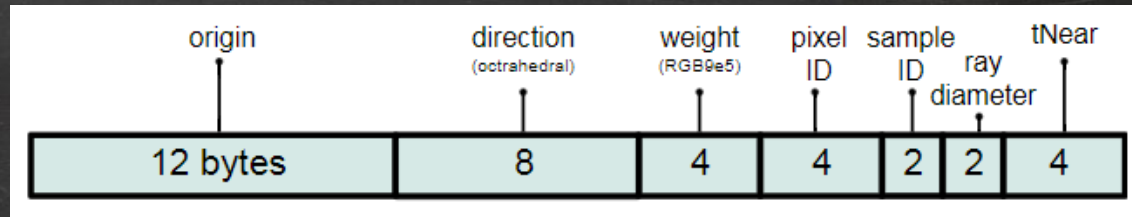
Core Ideas To Ensure Coherence

- Sort potentially out-of-core ray batches to extract ray groups from a complex scene
 - There are 30~60M rays per batch
 - Perform scene traversal per ray batch at a time
- Sort ray hits for deferred shading w.r.t. shading context (mesh ID + face ID)
 - Hit points are grouped by mesh ID, then sorted by face ID
 - Achieve sequential texture reads with PTex

Tracing Pipeline

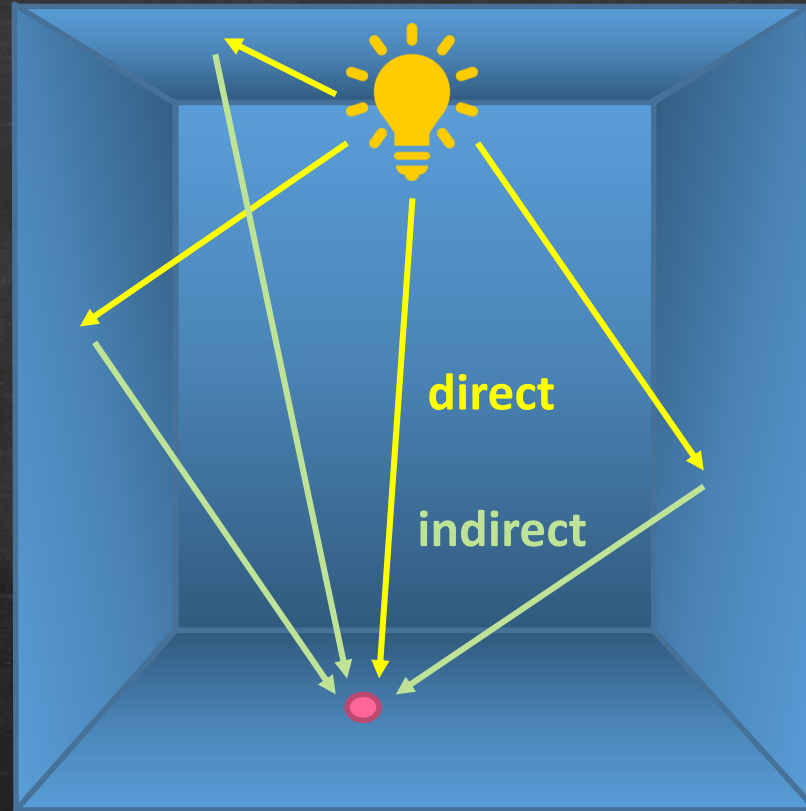


Tracing Pipeline

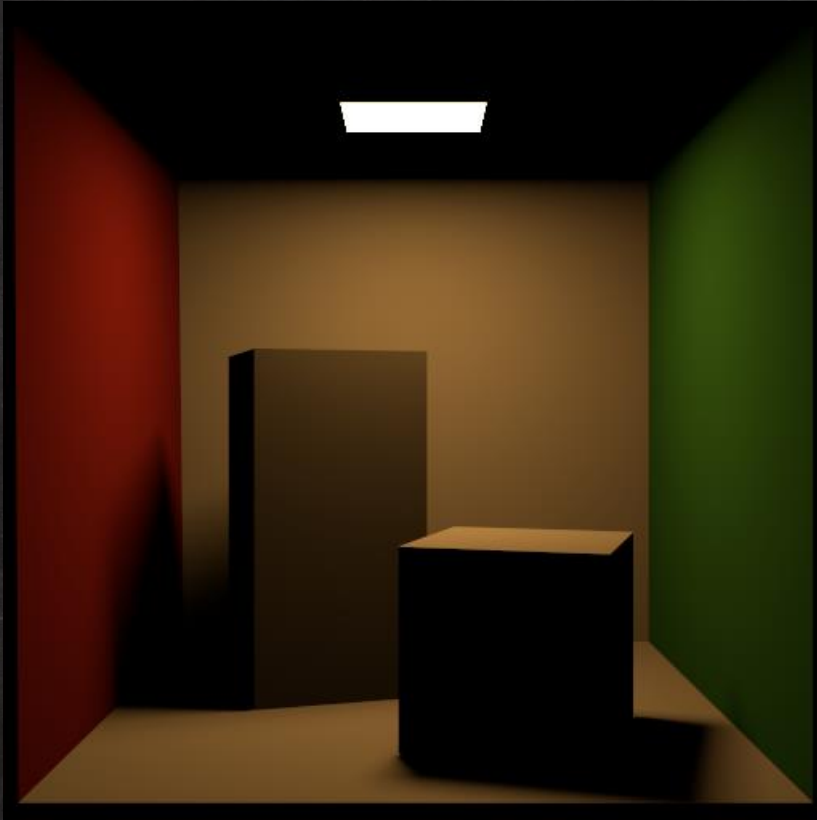


Render Equation

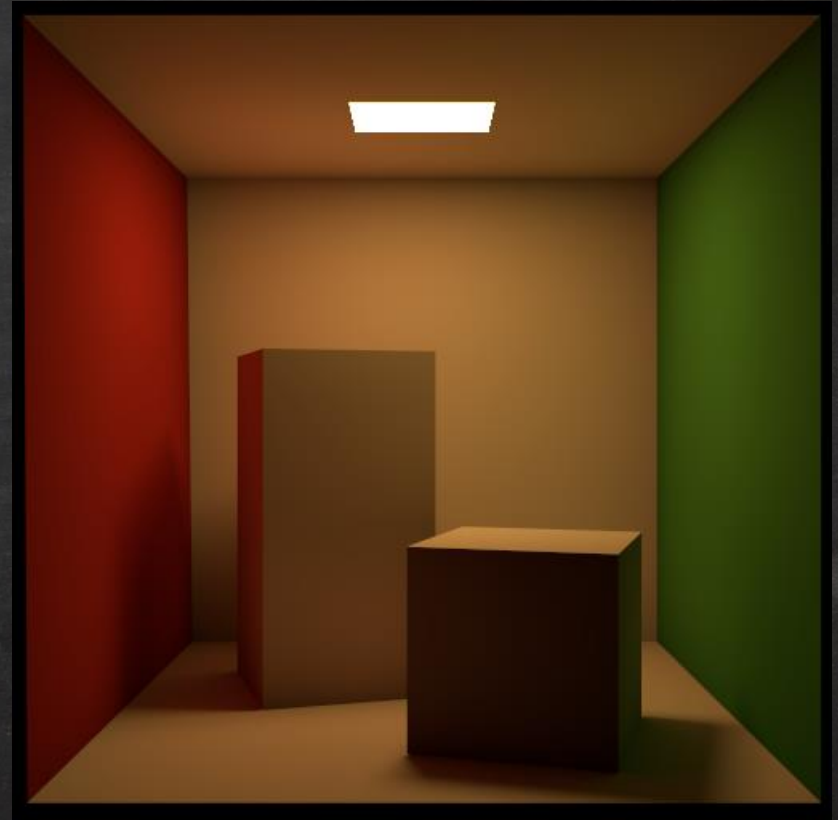
Where Does Light Come From?



Global = Direct + **Indirect** Lighting

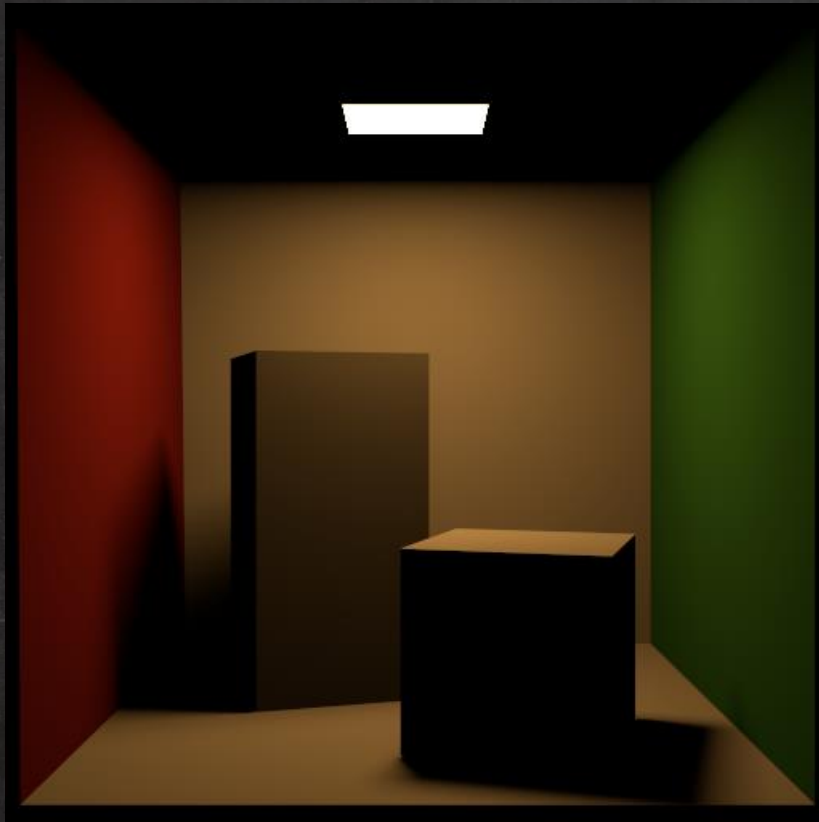


Direct Illumination

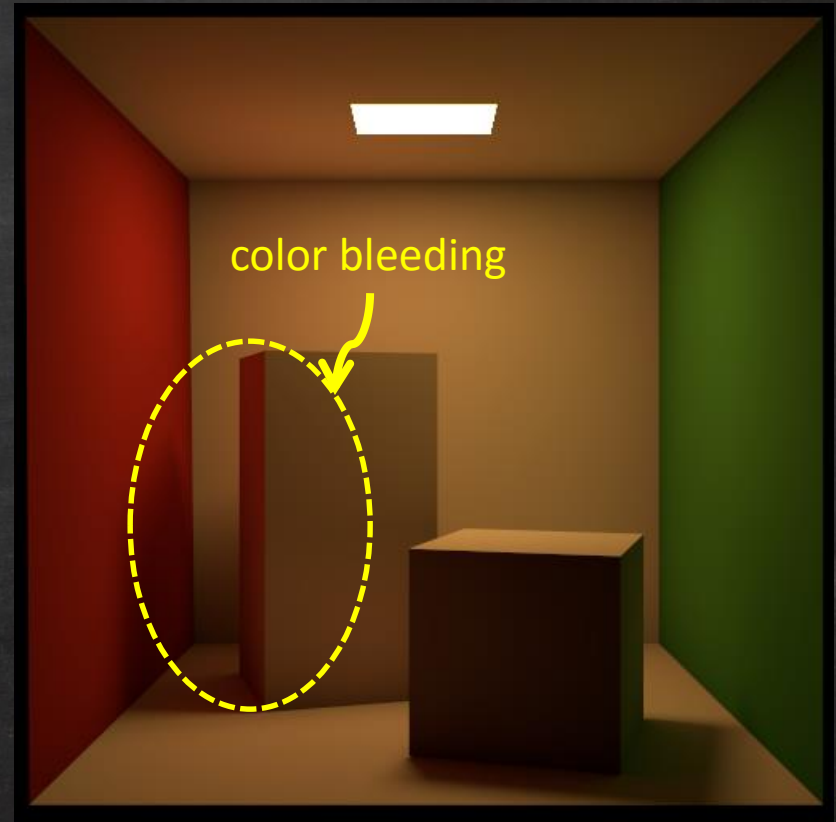


Global Illumination

Global = Direct + Indirect Lighting



Direct Illumination



Global Illumination

★ Render Equation

Unknown!!

$$L(x, \vec{\omega}_o) = L_e(x, \vec{\omega}_o) + \int_{\Omega} L(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n}) d\vec{\omega}_i$$

★ Render Equation

Unknown!!

$$L(x, \vec{\omega}_o) = L_e(x, \vec{\omega}_o) + \int_{\Omega} L(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n}) d\vec{\omega}_i$$



***How do we solve
this kind of equation??***

★ Render Equation

Unknown!!

$$L(x, \vec{\omega}_o) = L_e(x, \vec{\omega}_o) + \int_{\Omega} L(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n}) d\vec{\omega}_i$$

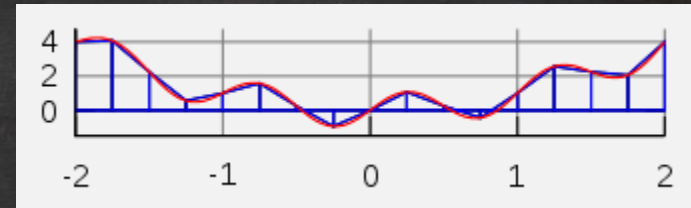
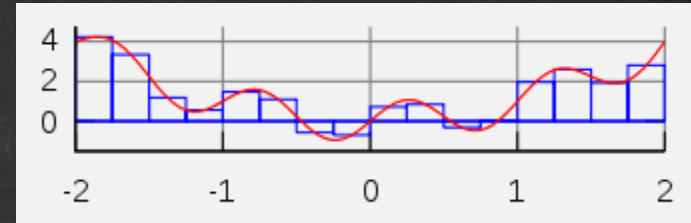


***How do we solve
this kind of equation??***



Quadrature

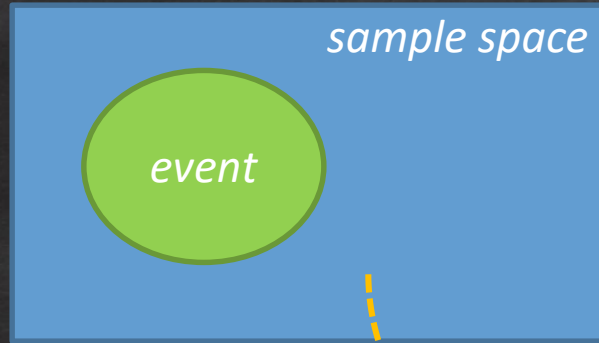
- 1D example
 - Rectangle/trapezoid
 - Gaussian quadrature
- Curse of dimensionality
 - The dimension of render equation is infinity!!
 - That's why we need Monte Carlo



Monte Carlo Integration



Probability Review



probability set function

$$P\left(\frac{E}{S}\right)$$

random variable
 $X: S \rightarrow \mathbb{R}$

It's a function, NOT a variable!!

Expected value of a random variable

$$E_p[f(x)] = \int f(x)p(x)dx$$

Variance

$$V[f(x)] = E[(f(x) - E[f(x)])^2]$$
$$V[f(x)] = E[(f(x))^2] - E[f(x)]^2$$

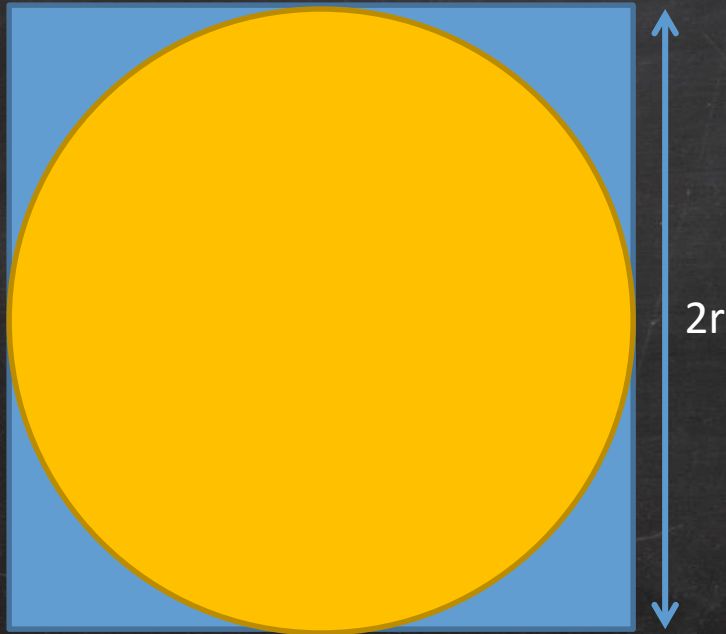
Concepts

- Use **random numbers** to approximate integrals
- It only estimates the values of integrals
 - i.e. gives the right answer **on average**
- It only requires to be able to evaluate the integrand at arbitrary points
 - Nice property for multi-dimensional integrand such as radiance in render equation

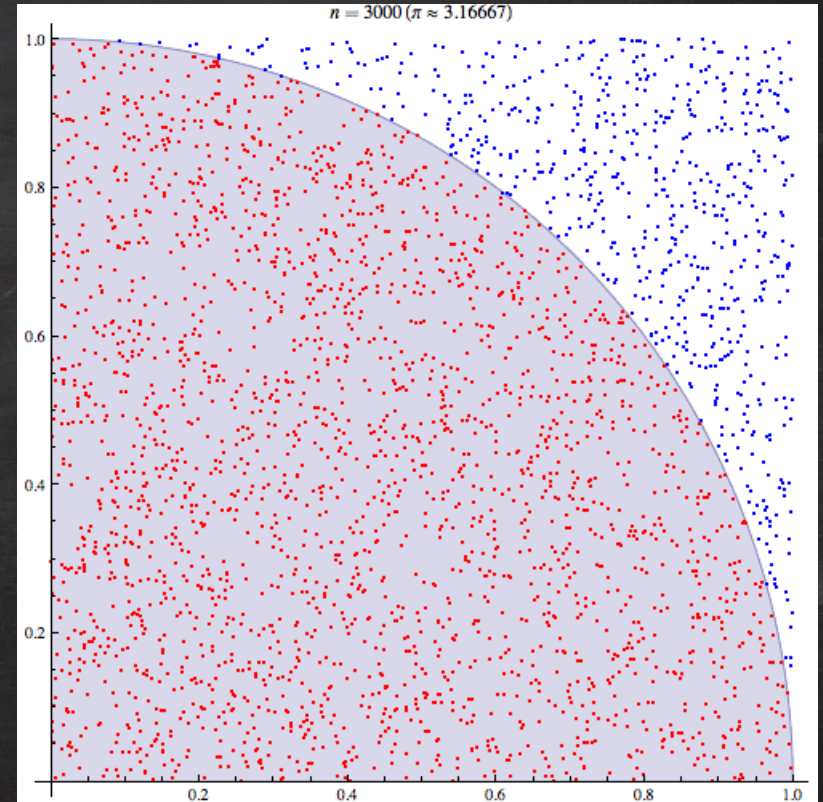
Monte Carlo Sampling

- ✓ Easy to implement
- ✓ Efficient for high dimensional integrals
- ✗ Noise (variance)
- ✗ Low convergence rate ($1/\sqrt{n}$)
 - But we don't have many other choices in high dimensional space!

Estimate π with Monte Carlo Sampling



$$P(\text{PointsInCircle}) = \frac{\pi r^2}{4r^2} \Rightarrow \pi = 4P$$



Probability Density Function (PDF)

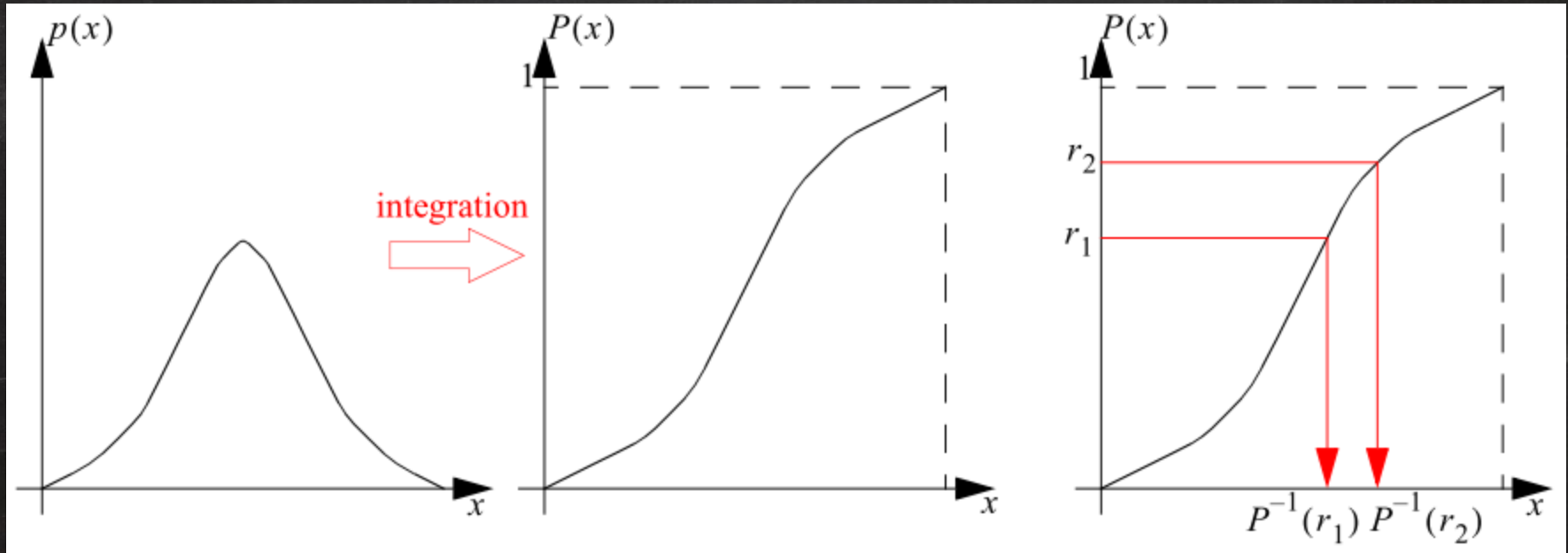
$$\Pr(x \in [a, b]) = \int_a^b p(x) dx$$

The relative probability of a random variable taking on a particular value

- $p(x) = \frac{d\Pr(x)}{dx} \geq 0$
- $\int_{-\infty}^{\infty} p(x) dx = 1, \Pr(x \in \mathbb{R}) = 1$

Cumulative Distribution Function (CDF)

$$P(x) = Pr\{X \leq x\}$$



Properties of Estimators

- Suppose Q is the unknown quantity
- Unbiased: $E[F_N] = Q$
 - Bias $\beta[F_N] = E[F_N] - Q$
 - The expected value is independent of sample size N
- Consistent
 - $\lim_{N \rightarrow \infty} \beta[F_N] = 0$
 - $\lim_{N \rightarrow \infty} E[F_N] = Q$

Law of Large Numbers

$$\Pr \left[\bar{E}(x) = \lim_{N \rightarrow \infty} \frac{1}{N} \sum_{i=1}^N x_i \right] = 1$$

$$\bar{E}[f(x)] \approx \frac{1}{N} \sum_{i=1}^N f(x_i)$$

Law of Large Numbers

N



$$\Pr \left[\left| \frac{1}{N} \sum_{i=1}^N X_i - \mu \right| > \epsilon \right] \rightarrow 0$$

$$E\left[\frac{1}{N} \sum_{i=1}^N f(X_i) \right] \rightarrow \int f(x) p(x) dx$$

Law of Large Numbers



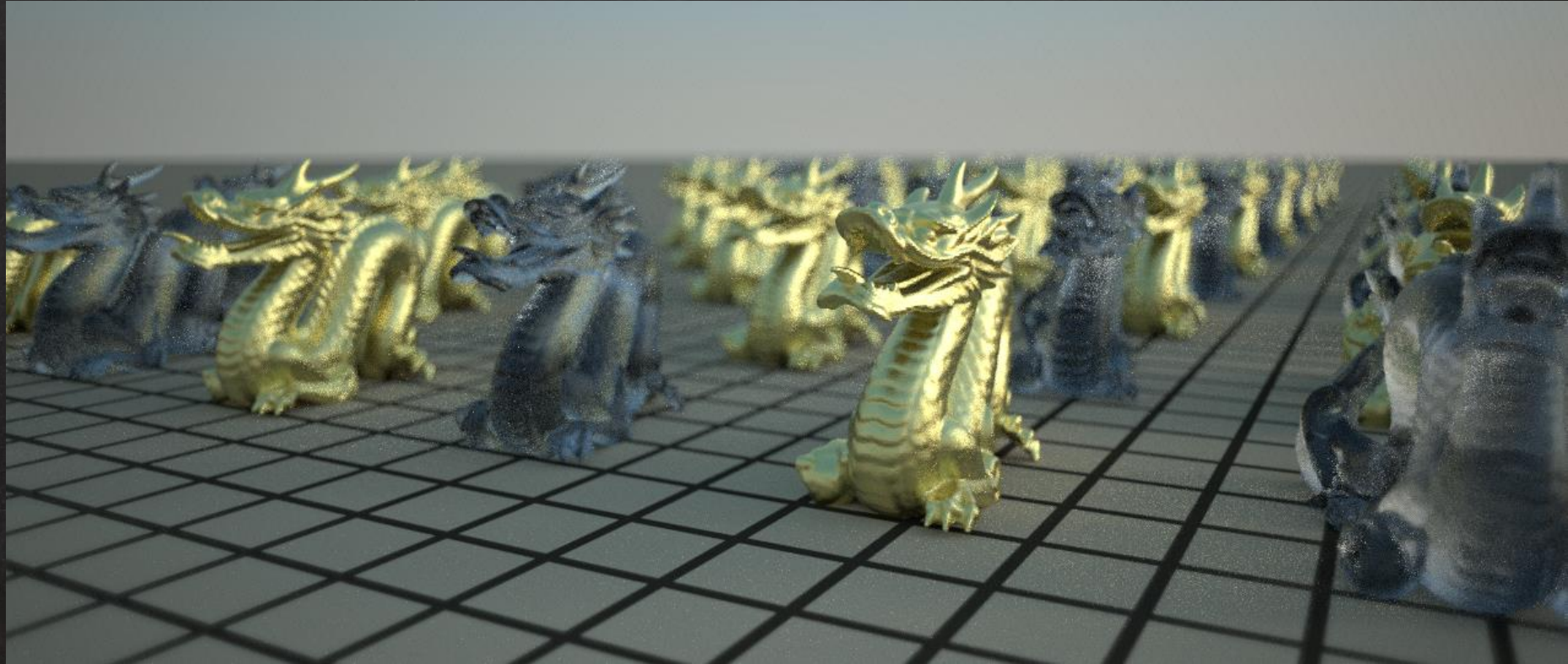
N



$$\Pr \left[\left| \frac{1}{N} \sum_{i=1}^N X_i - \mu \right| > \epsilon \right] \rightarrow 0$$

$$E\left[\frac{1}{N} \sum_{i=1}^N f(X_i) \right] = \mu$$

Insufficient Samples = High Variance = Noise



[Rendered with pbrt.v3]

Monte Carlo Estimation

$$\int f(x) dx = \int \frac{f(x)}{p(x)} p(x) dx = E \left[\frac{f(x)}{p(x)} \right] \approx \frac{1}{N} \sum_{i=1}^N \frac{f(x)}{p(x)}$$

estimator
↓

$$\int_{\Omega} L_i(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n}) d\vec{\omega}_i$$

≈

$$\frac{1}{N} \sum_{i=1}^N \frac{L_i(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n})}{p(\vec{\omega}_i)}$$

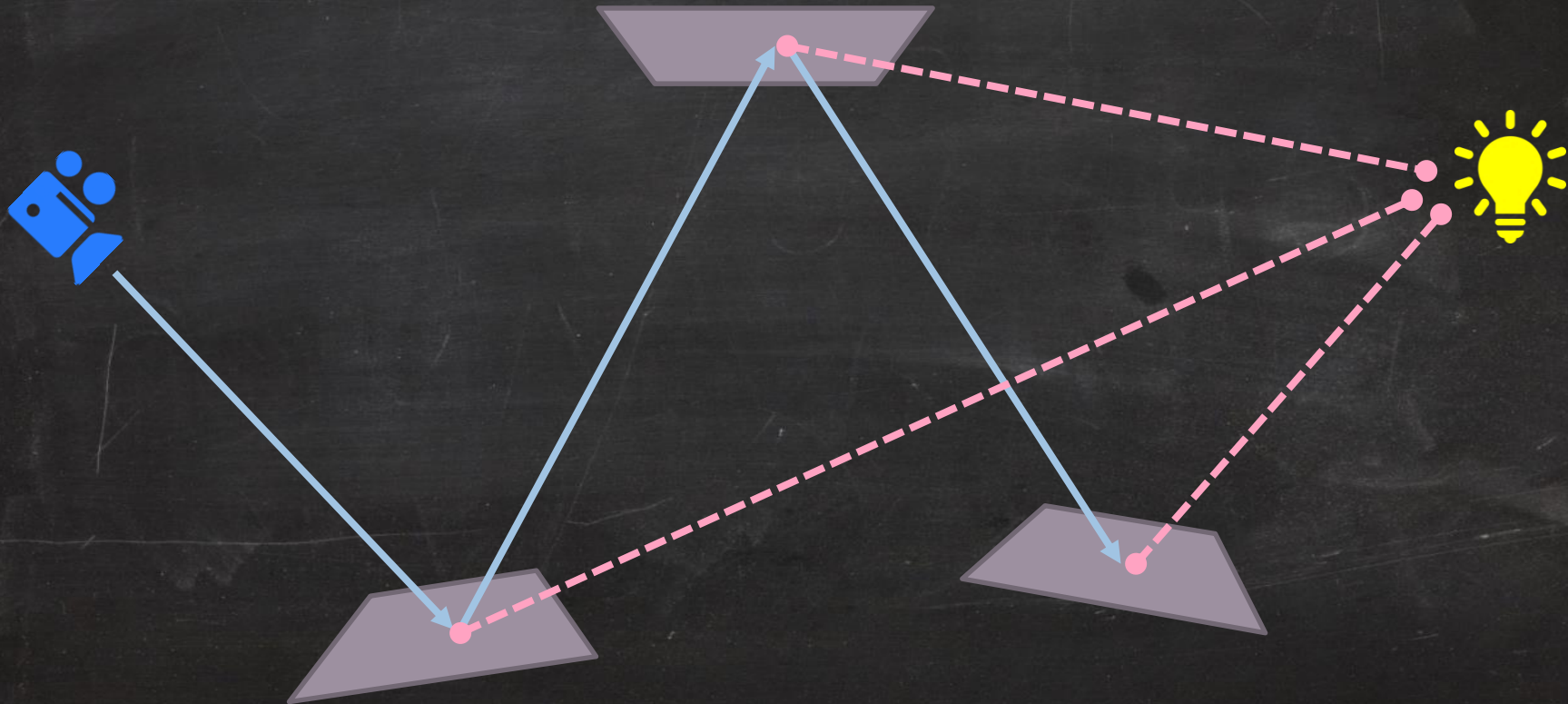
Tricky Part!!

Light Transport Algorithms

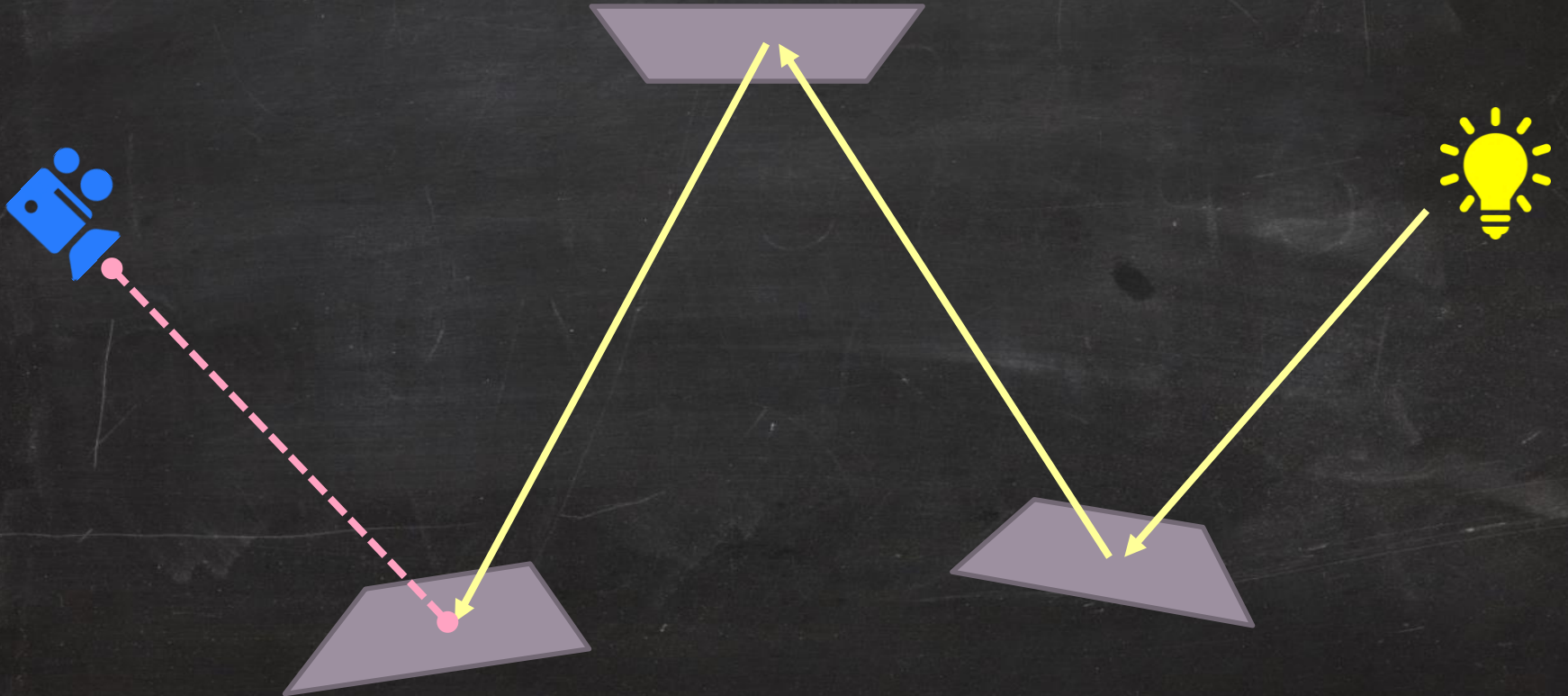
Light Transport Algorithms

- Path tracing
- Light tracing
- Bidirectional path tracing
- Photon mapping
- and many more...

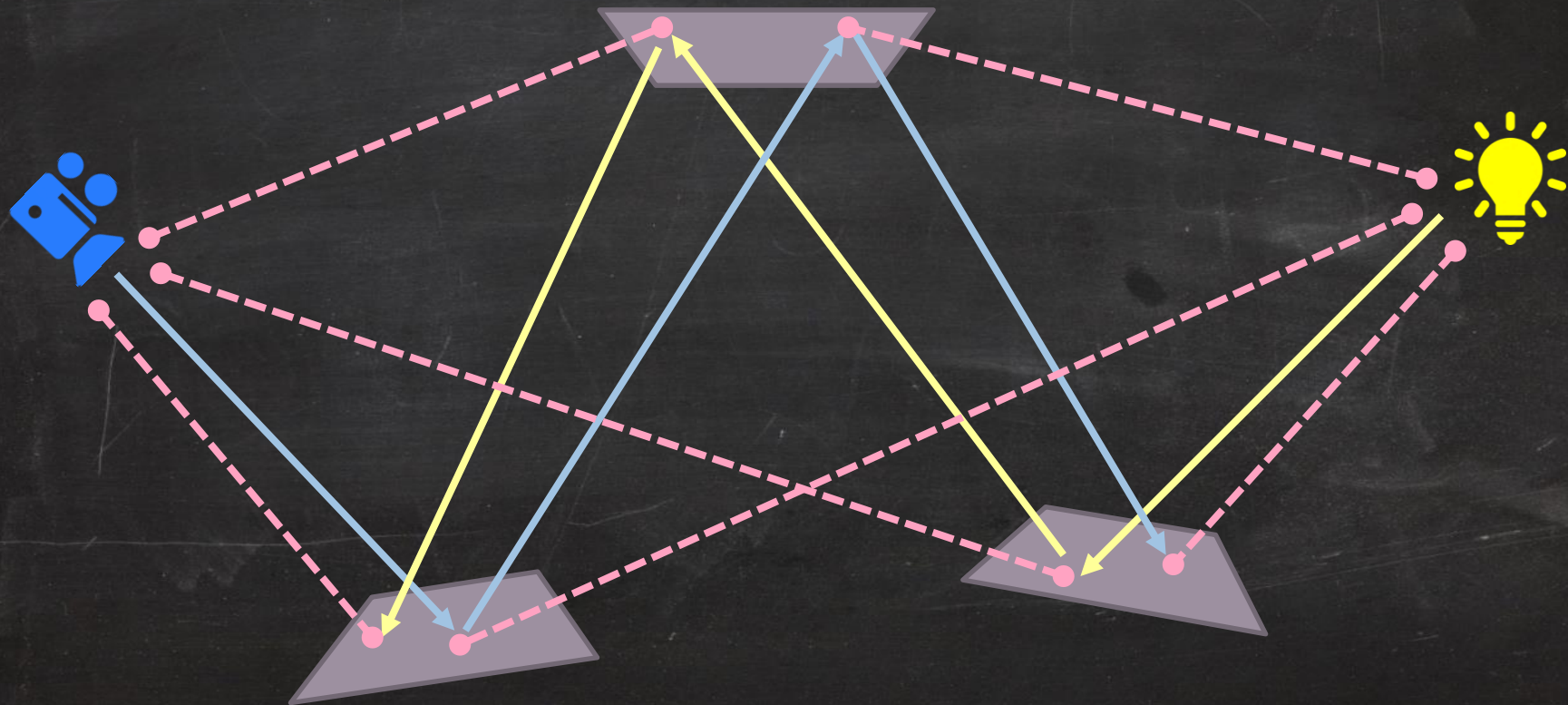
Path Tracing



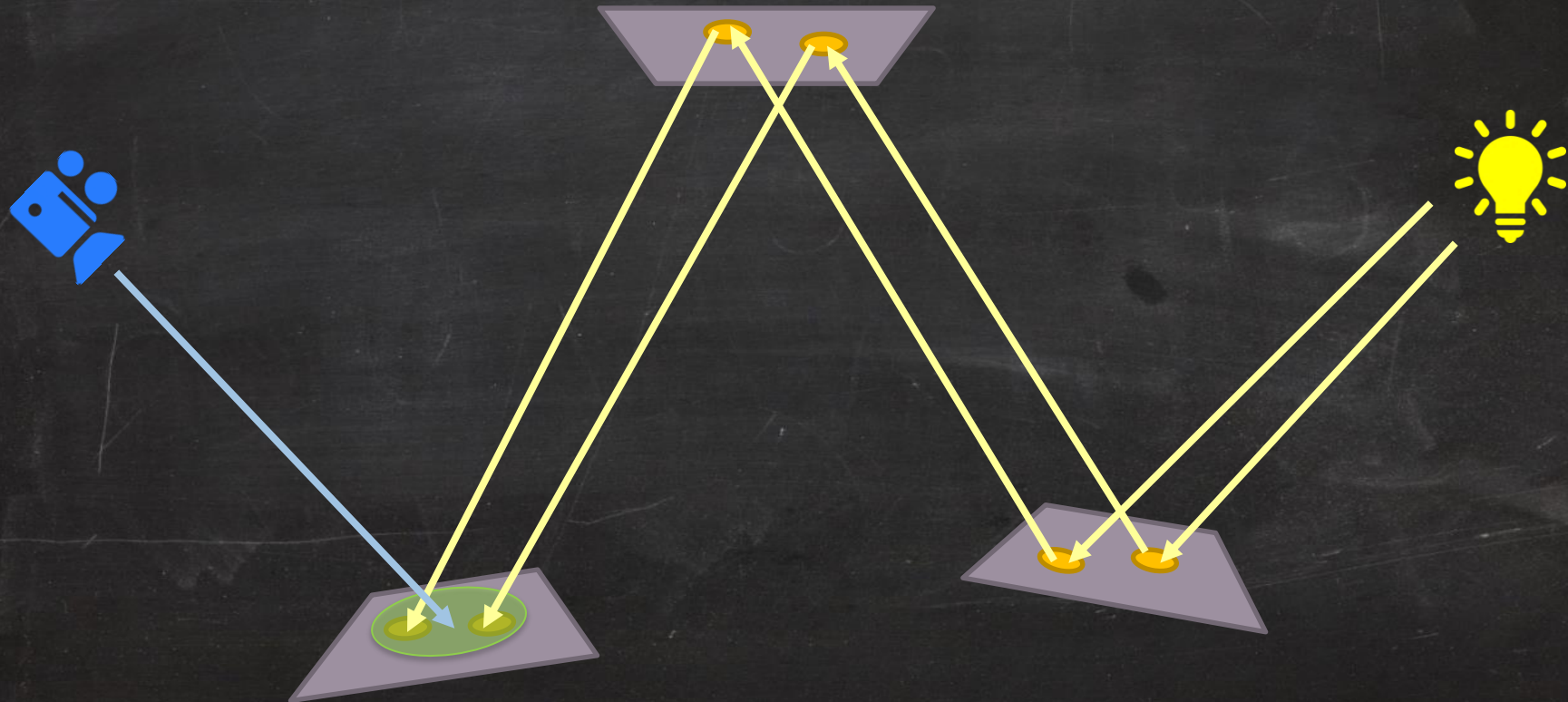
Light Tracing



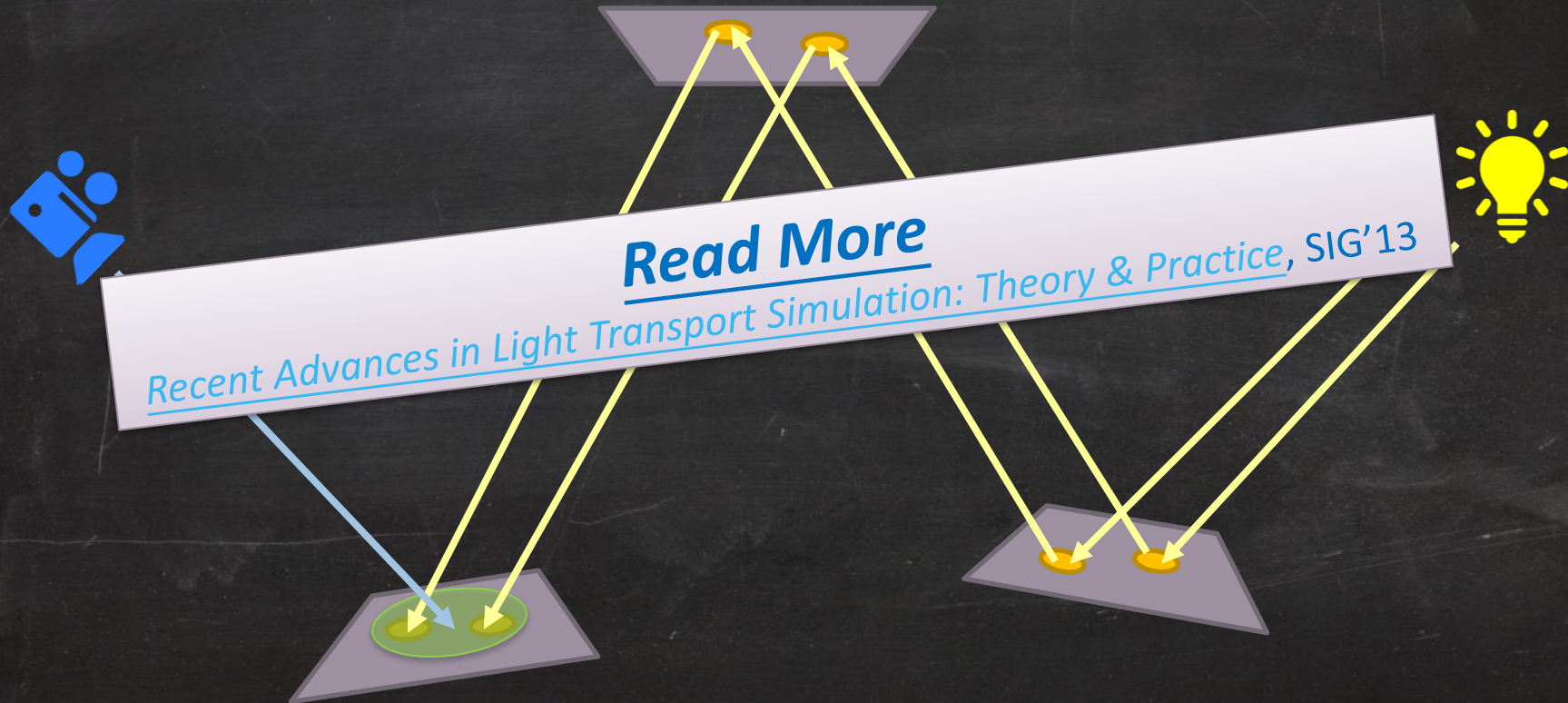
Bidirectional Path Tracing



Photon Tracing



Photon Tracing





Progressive Photon Mapping



Path Tracing



VCM

Bidirectional Path Tracing

Importance Sampling

Direct Illumination



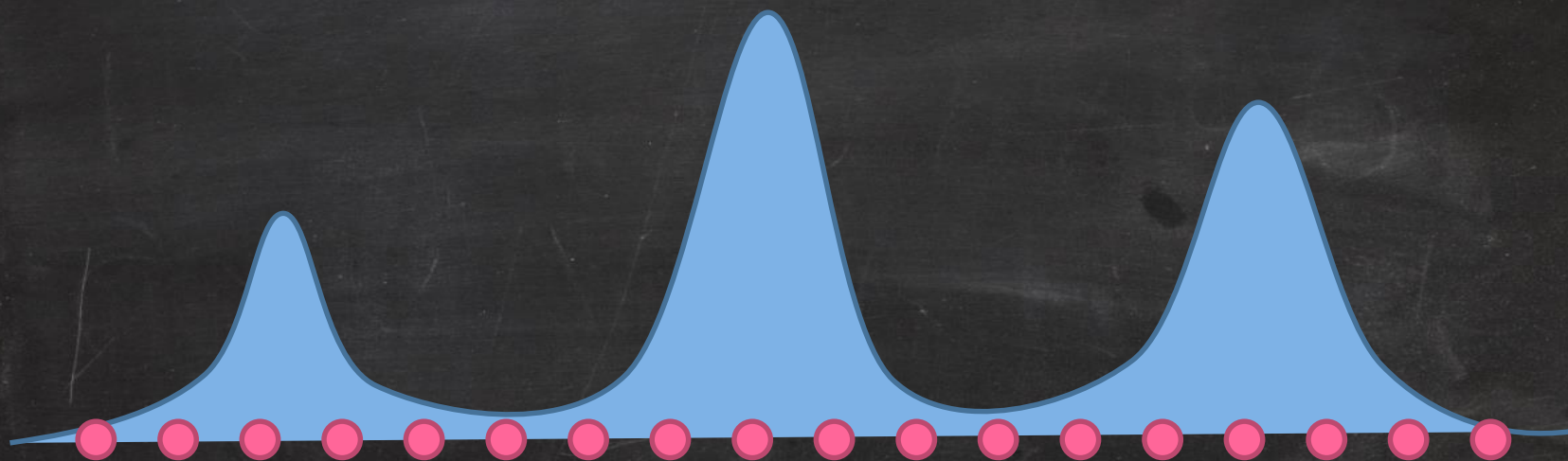
$$L_r(x, \vec{\omega}_o) = \int_{\Omega} L(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n}) d\vec{\omega}_i$$

≈

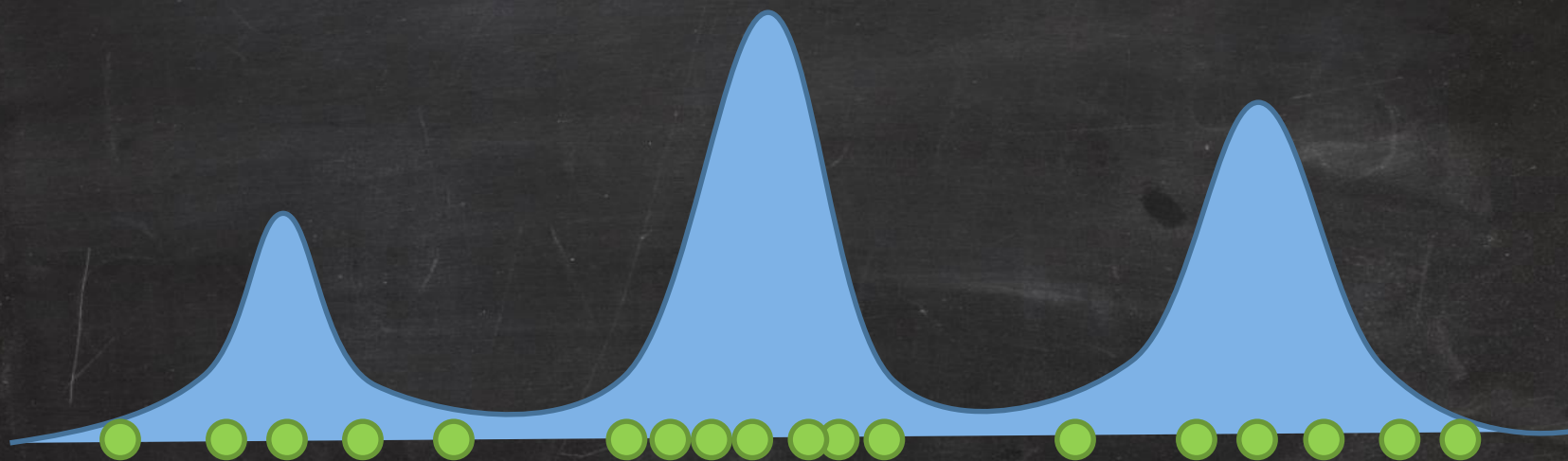
$$\frac{1}{N} \sum_{i=1}^N \frac{L_i(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n})}{p(\vec{\omega}_i)}$$

1. $p(\vec{\omega}_i) \propto L_i(x, \vec{\omega}_i) f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n})?$
2. $p(\vec{\omega}_i) \propto L_i(x, \vec{\omega}_i)?$
3. $p(\vec{\omega}_i) \propto f(\vec{\omega}_i, \vec{\omega}_o) (\vec{\omega}_i \cdot \vec{n})?$

Uniform Sampling



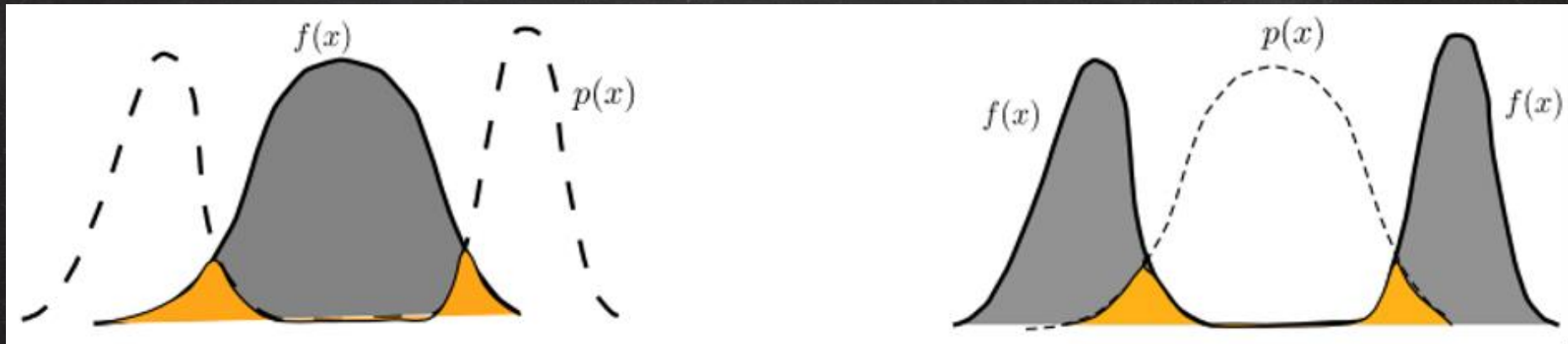
Importance Sampling



Importance Sampling (Cont'd)

$$F_N = \frac{1}{N} \sum \frac{f(X_i)}{p(X_i)},$$

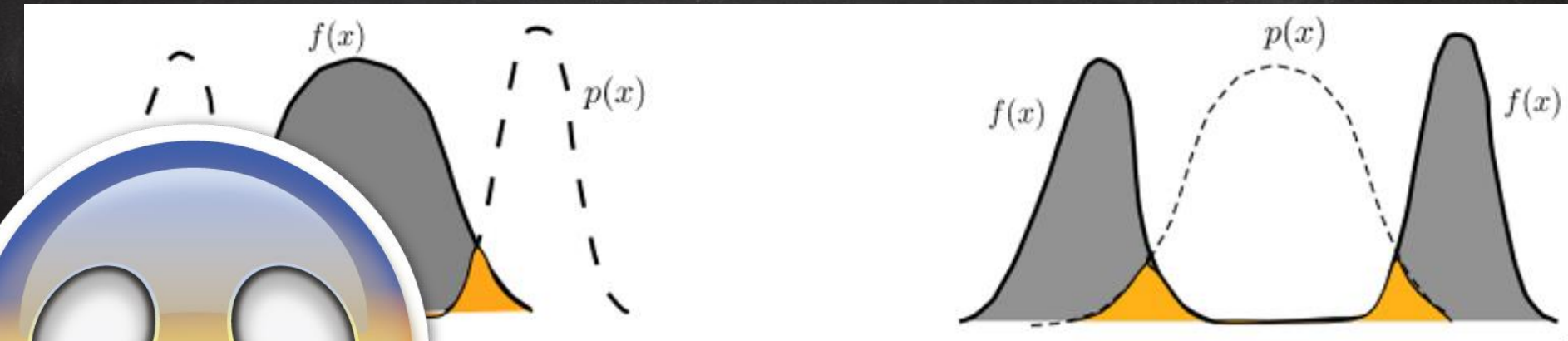
where $p(X_i) \propto f(X_i)$ **Unknown!!**



Importance Sampling (Cont'd)

$$F_N = \frac{1}{N} \sum \frac{f(X_i)}{p(X_i)},$$

where $p(X_i) \propto f(X_i)$ *Unknown!!*

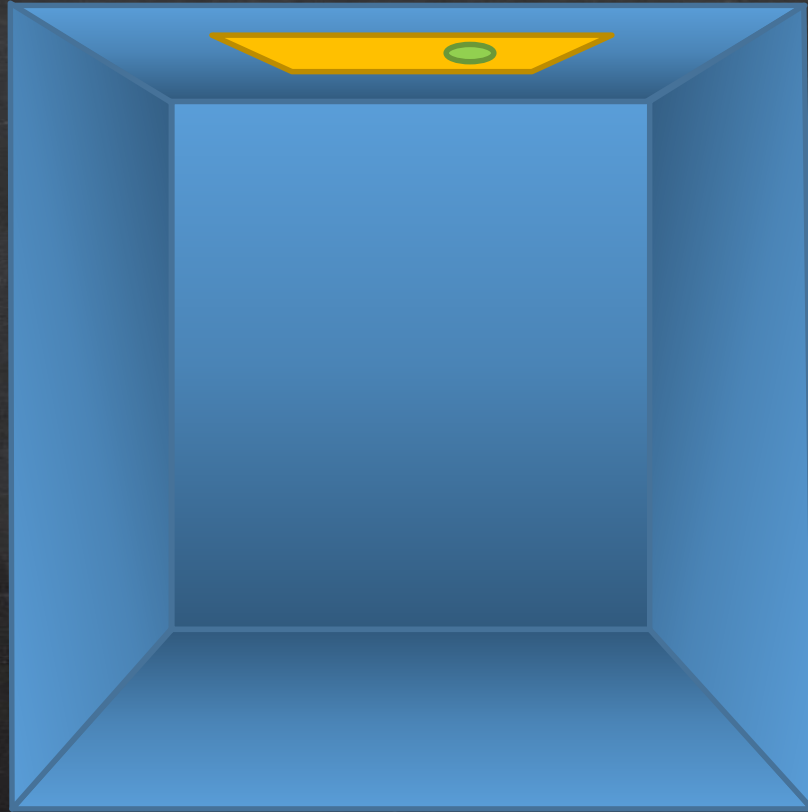


[Premože'10]

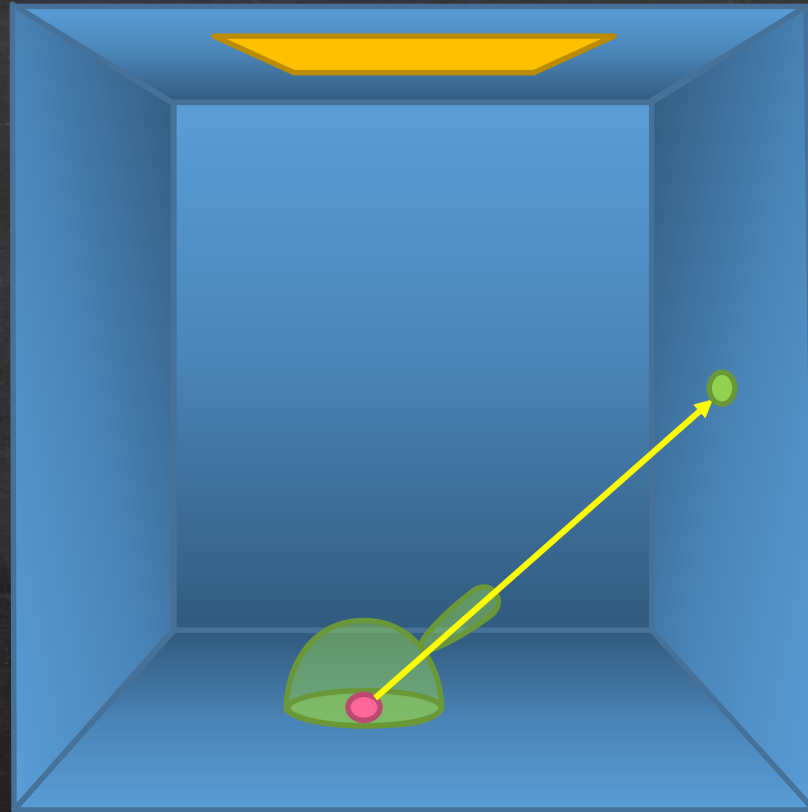
**Bad choice of density function
would increase the variance (to infinity)!!**



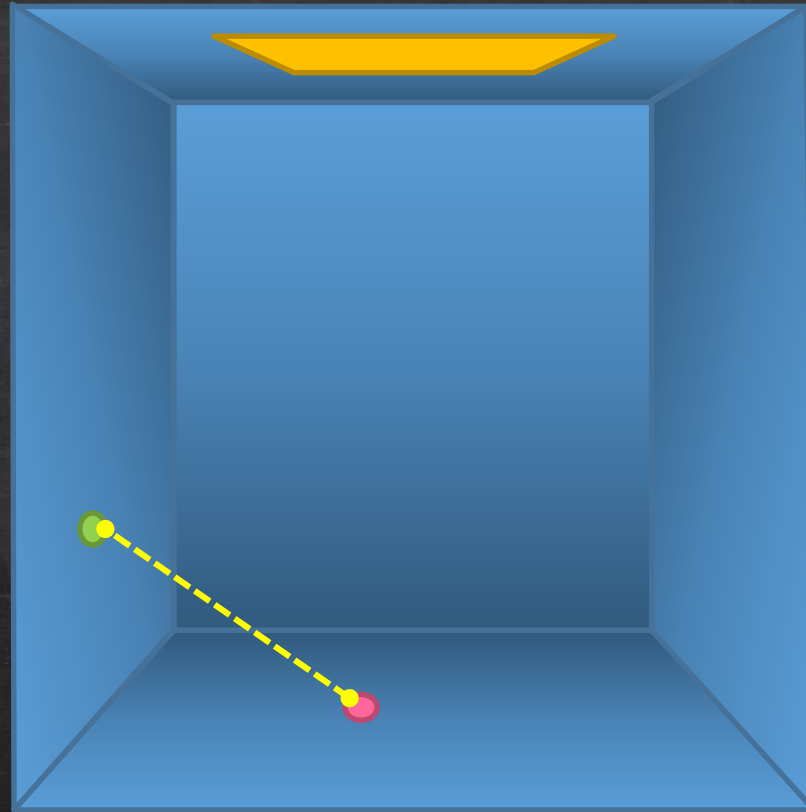
Emission Sampling



BRDF Sampling



High Throughput Connection

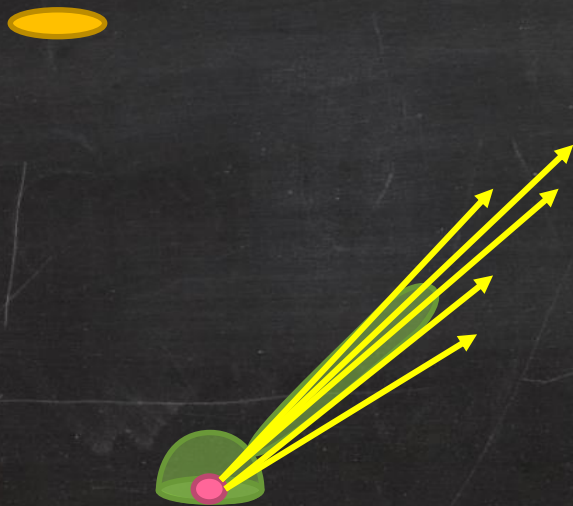


Challenges

- It's hard to get the PDF of the convolution of
 - Incoming radiance $L(x, \vec{\omega}_i)$ and
 - BRDF $f(\vec{\omega}_i, \vec{\omega}_o)$
- There's an implicit visibility term within $L(x, \vec{\omega}_i)$
 - Visibility term can't be derived before tracing
 - Using machine learning to adapt sampling distribution?
- Dilemma
 - Highly specular BRDFs with point light sources

Highly Specular BRDF & Point Light

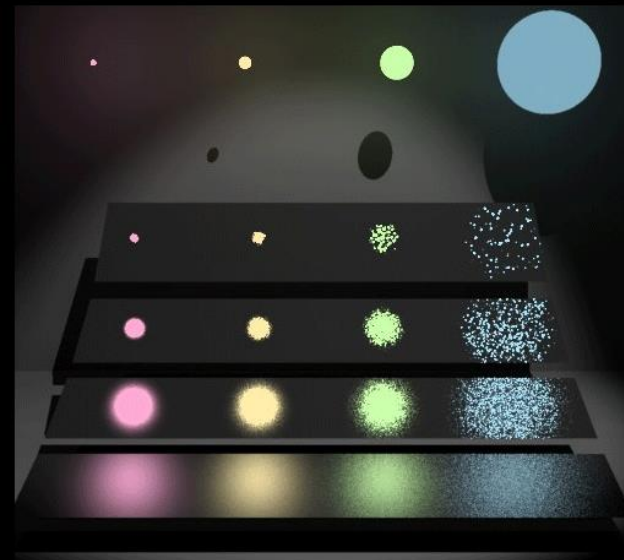
BRDF Sampling



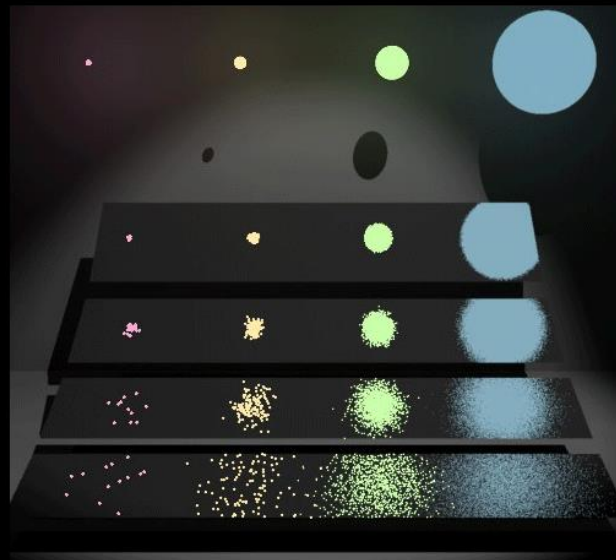
Light Sampling



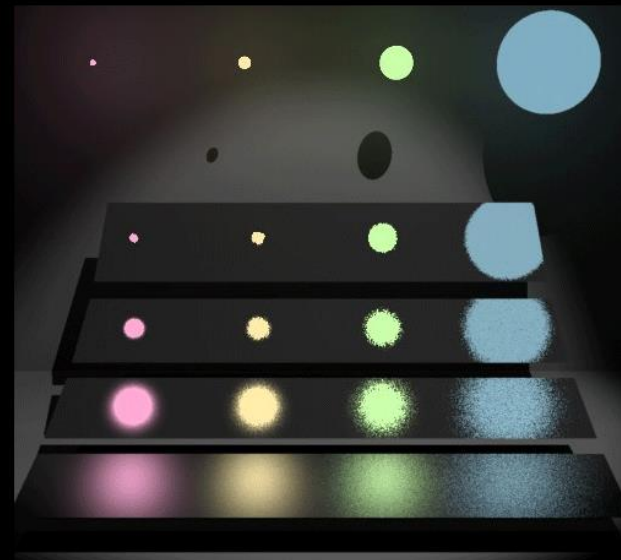
Multiple Importance Sampling



Sample Light Source



Sample BRDF



MIS with Power Heuristic

Multiple Importance Sampling (Cont'd)

$$\frac{1}{n_f} \sum_{i=1}^{n_f} \frac{f(X_i)g(X_i)w_f(X_i)}{p_f(X_i)} + \frac{1}{n_g} \sum_{j=1}^{n_g} \frac{f(Y_j)g(Y_j)w_g(Y_j)}{p_g(Y_j)}$$

- n_k is the number of samples taken from the p_k
- the weighting functions w_k take all of the different ways that a sample X_i or Y_i could have been generated

$$w_s(x) = \frac{n_s p_s(x)}{\sum_i n_i p_i(x)}$$

$$w_s(x) = \frac{(n_s p_s(x))^\beta}{\sum_i (n_i p_i(x))^\beta}$$

Multiple Importance Sampling (Cont'd)

$$\frac{1}{n_f} \sum_{i=1}^{n_f} f(X_i)g(X_i)w_f(X_i) + \frac{1}{n_g} \sum_{j=1}^{n_g} f(Y_j)g(Y_j)w_g(Y_j)$$

Read More

1. Robust Monte Carlo Methods for Light Transport Simulation,
Ch 2 & 9. Veach'97.

2. IS for Production Rendering, SIG'10

...actions w_k take all of the different ways
that a sample X_i or Y_i could have been generated

$$w_s(x) = \frac{n_s p_s(x)}{\sum_i n_i p_i(x)}$$

$$w_s(x) = \frac{(n_s p_s(x))^\beta}{\sum_i (n_i p_i(x))^\beta}$$